



Telangana State Board of
INTERMEDIATE Education

PHYSICS-I



BASIC LEARNING MATERIAL

For The Academic Year
2020-2021

TELANGANA STATE BOARD OF INTERMEDIATE EDUCATION



PHYSICS 1st YEAR (E/M)

BASIC LEARNING MATERIAL

ACADEMIC YEAR

2020-21

PREFACE

The ongoing Global Pandemic Covid-19 that has engulfed the entire world has changed every sphere of our life. Education, of course is not an exception. In the absence of Physical Classroom Teaching, Department of Intermediate Education Telangana has successfully engaged the students and imparted education through TV lessons. The actual class room teaching through physical classes was made possible only from 1st February 2021. In the back drop of the unprecedented situation due to the pandemic TSBIE has reduced the burden of curriculum load by considering only 70% syllabus for class room instruction as well as for the forthcoming Intermediate Public Examinations May 2021. It has also increased the choice of questions in the examination pattern for the convenience of the students.

To cope up with exam fear and stress and to prepare the students for annual exams in such a short span of time, TSBIE has prepared “Basic Learning Material” that serves as a primer for the students to face the examinations confidently. It must be noted here that, the Learning Material is not comprehensive and can never substitute the Textbook. At most it gives guidance as to how the students should include the essential steps in their answers and build upon them. I wish you to utilize the Basic Learning Material after you have thoroughly gone through the Text Book so that it may enable you to reinforce the concepts that you have learnt from the Textbook and Teachers. I appreciate ERTW Team, Subject Experts, Medha Charitable Trust who have involved day in and out to come out with the, Basic Learning Material in such a short span of time.

I would appreciate the feedback from all the stake holders for making it enriching and cent percent error free in all aspects.

The material can be accessed through our website www.tsbie.cgg.gov.in which is exclusively devoted to uploading the additional study material from time to time.

Commissioner & Secretary
Intermediate Education, Telangana.

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PHYSICAL WORLD

VERY SHORT QUESTION & ANSWERS (2 MARKS)

1. What is Physics?

Ans:- Physics is a branch of science which deals with the study of nature and natural phenomena. It deals with Motion, energy and their consequences.

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2. What are the fundamental forces in nature?

Ans:- Basic forces in nature are of the 4 types :

- | | |
|--------------------------|----------------------------|
| 1) Gravitational forces. | 2) Electromagnetic Forces. |
| 3) Weak nuclear Forces. | 4) Strong Nuclear Forces. |



UNIT II

UNITS AND MEASUREMENTS

VERY SHORT QUESTION & ANSWERS (2 MARKS)

1. Distinguish between accuracy and precisions.

Ans:-	<p>Accuracy</p> <p>1) Accuracy of a measurement is a measure of how close the measured value is to the true value of quantity.</p>	<p>Precision</p> <p>1) Whereas precision tells us to what resolution or what resolution or limit the quantity is measured. It depends on the resolution of the measuring devices.</p>
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2. What are the different types of errors that can occur in a measurement?

Ans:- Mainly there are three types of errors :

- 1) Systematic errors 2) Random error 3) Gross error.

3. How can systematic errors can be minimised or eliminated?

Ans:- Systematic, selecting better instruments and removing personal bias as far as possible.

4. Illustrate how the result of a measurement is to be reported indicating the error involved?

Ans:- Errors are uncertainties that are present in the measurement made with any measuring instrument, least count of instrument is minimum error in the measurement.

5. What are significant figures and what do they represent when reporting the result of a measurement?

Ans:- The digits of numbers that are definitely known plus one more digit that is estimated are called significant digit.

Example : The time period of a simple pendulum is 1.62 s. The digit 1 and 6 are reliable while the digit 2 is uncertain. The measured value has three significant figures.

6. Distinguish between fundamental units and derived units?

Ans:- a) Units of fundamental physical quantities, such as length, mass, time, etc., are known as fundamental units.

b) Units of the derived physical quantities, such as velocity, force, energy, etc., are known as derived units.

7. Why do we have different units for the same physical quantities?

Ans:- The result of a measurement of a physical quantity is expressed by a number accompanied by a unit.

8. What is dimensional analysis?

Ans:- 1) Dimensional analysis is the representation of derived physical quantities in terms of units of fundamental quantities.

2) With the help of dimensional analysis to check the correctness of the equation. Convert one system of units into the other system and derive certain equation relating physical quantities.

9. How many orders of magnitude greater is the radius of the atom as compared to that of the nucleus?

Ans:- Size of nucleus = 10^{-14} m, size of atom = 10^{-10} m

Hence size of atom is 10^4 m greater than the size of the nucleus.

10. Express unified atomic mass unit in Kg.

Ans:- 1 unified atomic mass unit = $\frac{1}{12}$ of the mass of carbon - 12 atom.

1 amu = 1.66×10^{-27} Kg

SHORT QUESTION & ANSWERS (4 MARKS)**1. The vernier scale of an instrument has 50 divisions which coincide with 49 main scale divisions. If each main scale division is 0.5mm, then using this instrument that would be the minimum in accuracy in the measurement of distance?**

Ans:- Value of each main scale division = 0.5mm

No. of vernier scale division = 50

In vernier callipers $L.C. = \frac{S}{N} = \frac{\text{Value of one main scale division}}{\text{No. of vernier scale division}}$

$$L.C. = \frac{0.5}{50} = 0.01\text{mm}$$

The minimum in accuracy in the measurement of distance is 0.1 mm.

2. In a system of units, the unit of force is 100N unit of length is 10m and the unit of time is 100s. What is the unit of mass in this system?

Ans:- Force = 100N, length = 10m Time = 100 sec.

$F = ma$

$$m = \frac{F}{a} = \frac{F}{LT^{-2}} = \frac{F.T^2}{L} = \frac{100 \times 100 \times 100}{10} = 10^5 \text{ kg}$$

3. The distance of a galaxy from Earth is of the order of 10^{25} m . Calculate the order of magnitude of the time taken by light to reach us from the galaxy?

Ans:- Distance of galaxy from earth = 10^{25} m

Velocity of light = $3 \times 10^8 \text{ m/s}$

$$\text{Time taken by the light} = \frac{\text{Velocity of light}}{\text{Distance of galaxy from earth}}$$

$$= \frac{d}{v} = \frac{10^{25}}{3 \times 10^8} = 0.33 \times 10^7 = 3.3 \times 10^{16} \text{ sec}$$

4. The Earth moon distance is about 60 Earth radius. What will be the approximate diameter of the earth as seen from the moon?

Ans:- Distance between earth moon = $60 R$

Radius of earth = R

$$r = 60 R = 60 \times 6400 \times 10^3 \text{ (R=6400 km)}$$

$$\theta = 1 \text{ sec} = \frac{1}{60} \text{ min} = \frac{1}{60 \times 60} \text{ degree}$$

$$= \frac{1}{60 \times 60} \times \frac{\pi}{180} \text{ radian}$$

$$r = \frac{l}{\theta} \Rightarrow l = r \times \theta = 60 \times 6400 \times 10^3 \times 60 \times 60 \times \frac{\pi}{180}$$

$$l = 11.16 \times 10^3 \text{ km} \Rightarrow \text{Diameter } l = 11.16 \times 10^3 \text{ km}$$

5. Three measurements of the time for 20 oscillations of a pendulum give $t_1 = 39.6 \text{ s}$, $t_2 = 39.9 \text{ s}$ and $t_3 = 39.5 \text{ s}$ what is the precision in the measurements? What is the accuracy of the measurements?

Ans:- No. of oscillations = 20

$$t_1 = 39.6 \text{ sec}, t_2 = 39.9 \text{ sec}, t_3 = 39.5 \text{ sec}$$

$$\begin{aligned} \text{Mean value} &= \frac{t_1 + t_2 + t_3}{3} = \frac{39.6 + 39.9 + 39.5}{3} \\ &= 39.66 \approx 39.7 \text{ sec} \end{aligned}$$

$$\text{Precision} = 0.1 \text{ sec}$$

Accuracy is the closeness of measured value with true value

Hence 39.6 sec is accurate.

6. 1 Caloric = 4.2 where $1\text{J} = 1\text{Kg m}^2\text{s}^{-2}$ suppose we employ a system of units in which the unit of mass is \hat{a} kg the unit of length is \hat{a} m and the unit of time is \hat{a} s, show that a caloric has a magnitude $4.2 \hat{a}^{-1} \hat{a}^2 \hat{a}^{-2}$ in the new system?

Ans:- $1 \text{ caloric} = 4.2\text{J} \Rightarrow 1\text{J} = 1\text{kg m}^2\text{s}^{-2}$

$$1 \text{ caloric} = 4.2 \text{ Kg.m}^2\text{s}^{-2}$$

$$\text{In a new system } 1 \text{ caloric} = 4.2 \hat{a} \hat{a}^2 \hat{a}^{-2}$$

7. A new unit of length is chosen so that the speed of light in vacuum is 1ms^{-1} . If light takes 8 min and 20 s to cover this distance, what is the distance between the sun and earth in terms of the new unit?

Ans:- $V = \text{speed of light in vacuum} = 1\text{m/s}$

$$\text{Time taken (t)} = 8 \text{ min } 20 \text{ sec} = 500 \text{ sec.}$$

$$\text{Distance between the sun and earth} = \frac{V}{t} = \frac{1}{500} = 0.002\text{m}.$$

8. A student measured the thickness of a human hair using a microscope of magnification 100. He makes 20 observations and finds that the average thickness (as viewed in the microscope) is 3.5 mm, what is the estimate of the thickness of hair?

Ans:- Magnification of microscope = $m = 100$

$$\text{observed thickness} = 3.5 \text{ mm}$$

$$\text{magnification} = \frac{\text{observed thickness}}{\text{Real thickness}}$$

$$100 = \frac{3.5}{\text{Real thickness (t)}}$$

$$t = \frac{3.5}{100} = 0.035\text{mm}$$

9. A physical quantity x is related to four measurable quantities a, b, c and d as follows. $x = a^2 b^3 c^{5/2} d^{-2}$ the percentage error in the measurement of a, b, c, d are 1%, 2%, 3%, 4% respectively, what is the percentage of error in x ?

Ans:- $x = a^2 b^3 c^{5/2} d^{-2}$

$$\frac{\Delta a}{a} \times 100 = 1\%, \quad \frac{\Delta b}{b} \times 100 = 2\%, \quad \frac{\Delta c}{c} \times 100 = 3\%, \quad \frac{\Delta d}{d} \times 100 = 4\%$$

Percentage error in x is

$$\left(\frac{\Delta x}{x} \right) \times 100 = 2 \left(\frac{\Delta a}{a} \times 100 \right) + 3 \left(\frac{\Delta b}{b} \times 100 \right) + \frac{5}{2} \left(\frac{\Delta c}{c} \times 100 \right) + 2 \frac{\Delta d}{d} \times 100$$

$$= 2 \times 1 + 3 \times 2 + \frac{5}{2} \times 3 + 2 \times 4 = 2 + 6 + \frac{15}{2} + 8$$

$$= 23.5 \%$$

10. The velocity of a body is given by $v = A^{+2} + B^{+} + C$. If v and t are expressed in SI what are the units of A , B and C ?

Ans:- Given $V = At^2 + Bt + C$

According to principle of homogeneity

$$\text{i) } V = At^2 \Rightarrow A = \frac{V}{t^2} = \frac{LT^{-1}}{T^2} = LT^{-3} = \text{ms}^{-3}$$

$$\text{ii) } V = Bt \Rightarrow B = \frac{V}{t} = \frac{LT^{-1}}{T^1} = LT^{-2} = \text{ms}^{-2}$$

$$\text{iii) } V = C \Rightarrow C = LT^{-1} = \text{ms}^{-1}$$

Problems :

1. In the expression $p = EL^2m^{-5}G^{-2}$ the quantities. E , L , m and G denote energy, angular momentum, mass and gravitational constant respectively. Show that p is a dimensionless quantity.

<p>Sol. $P = EL^2 m^{-5} G^{-2}$</p> $P = [ML^2T^{-2}] [ML^2T^{-1}]^2 [M^5] [M^{-1}L^3T^{-2}]$ $P = M^{1+2-5+2} L^{2+4-6} T^{-2-2+4}$ $P = [M^0 L^0 T^0]$	$\left \begin{array}{l} E = [M L^2 T^{-2}] \\ L = [M L^2 T^{-1}] \\ M = [M] \\ G = [M] \end{array} \right.$
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\therefore Hence P is dimensionless quantity.

2. An artificial satellite is revolving around a planet of Mass M and radius R in a circular orbit of radius r using dimensional analysis show that the period of the satellite? $T = \frac{K}{R} \sqrt{\frac{r^3}{g}}$ when K is a dimensionless constant and g is acceleration due to gravity.

<p>Sol. $T = \frac{K}{R} \sqrt{\frac{r^3}{g}}$</p> <p>L.H.S = Time period = T,</p>	$\left \begin{array}{l} \\ \\ \\ \end{array} \right.$	$\text{R.H.S} = \frac{K}{R} \sqrt{\frac{r^3}{g}} = \frac{1}{L} \sqrt{\frac{L^3}{LT^{-2}}} = T$
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\therefore L.H.S = R.H.S

above equations is correct.

3. The error in measurement of radius of a sphere is 1% what is the error in the measurement of volume?

Sol. Radius of sphere $\frac{\Delta r}{r} \times 100 = 1\%$

$$\text{Volume } V = \frac{4}{3} \pi r^3$$

$$\frac{\Delta V}{V} \times 100 = 3 \times \frac{\Delta r}{r} \times 100 = 3 \times 1\% = 3\%$$



UNIT III

MOTION IN A STRAIGHT LINE

VERY SHORT QUESTION & ANSWERS (2 MARKS)

1. The states of motion and rest are relative. Explain.

Ans:- Rest and motion are relative. They are not absolute. A body can be in the rest or in motion with respect to reference frame. A man in a moving train is at rest with respect to a co-passenger but he is in motion with respect to a man on the ground.

2. How is average velocity different from instantaneous velocity?

Ans:- The average velocity does not give any detail of the motion of the particle. It gives only the result of the motion. The instantaneous velocity defines how fast the particle moves at a particular instant of time.

In uniform motion the instantaneous velocity is equal to the average velocity.

3. Give an example where the velocity of an object is zero but its acceleration is not zero?

Ans:- When the body is projected vertically upwards at the highest point its velocity is zero. But acceleration, ($a=g$) is not equal to zero.

4. A vehicle travels half the distance L with speed V_1 and the other half with speed V_2 , what is the average speed?

Ans:- Average speed = $\frac{\text{Total length of the path}}{\text{Total time taken}}$

$$= \frac{L}{\left(\frac{L}{2}\right) \frac{1}{V_1} + \left(\frac{L}{2}\right) \frac{1}{V_2}} = \frac{2V_1V_2}{V_1 + V_2}$$

5. A lift coming down is just about to reach the ground floor. taking the ground floor as origin and +ve direction upwards for all quantities, which one of the following is correct.

(a) $x < 0$, $v < 0$, $a > 0$

(b) $x > 0$, $v < 0$, $a < 0$

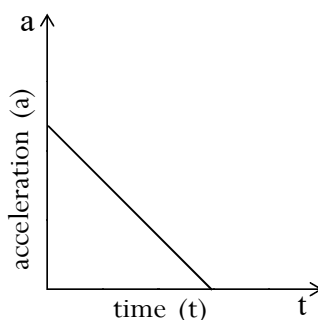
(c) $x > 0$, $v < 0$, $a > 0$

(d) $x > 0$, $v > 0$, $a > 0$

Ans:- While lift is moving towards ground floor. Conigin +ve x decresses velocity decneases. Hence $x < 0$, $v < 0$, but $a > 0$ so (a) is correcet option.

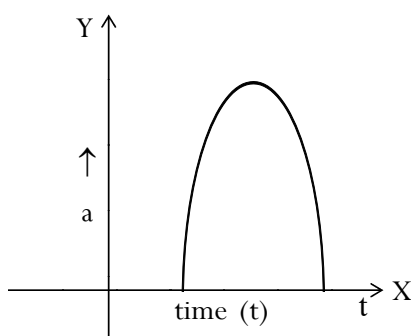
6. A uniformly moving cricket ball is lit with a bt for a very short fime and is turned back. Show the variation of its acceleration with time taking the accelpration in the backward direction as positive.

Ans:-



7. Give an example of one dimensions motion where a particle moving along the positive x-direction. comes to rest periodically and moves for ward?

Ans:-



8. An object falling through a flnid is observed to have an acceleration given by $a = g - bv$ where g is the gravitional acceleration and b is a constant. After a long time it is observed to fall with a constant velocity. What would be the value of this constant velocity?

Ans:- $a = g - br$

$$\frac{dv}{dt} = g - br$$

$$0 = g - br \quad \Rightarrow \quad v = \frac{g}{b}$$

9. If the trajectory of a body is parabolic in one frame can it be parabolic in another frame that moves with a constant velocity with respect to the first frame? It not what can it be?

Ans:- No, the trajectory is vertical straight line.

10. A Spring with one end attached to a mass and the other to a rigid support is stretched and released when is the magnitude of a acceleration a maximum?

Ans:- The magnitude of acceleration is maximum at Extreme positions.

SHORT QUESTION & ANSWERS (4MARKS)

1. Can the equations of kinematics be used when the acceleration varies with time? If not, what form would these equation take?

Ans:- No, the equation of Kinematics be used when the acceleration varies with time.

If an object moves along a straight line with uniform acceleration (a) equations of Kinematics are.

$$(1) V = V_0 + at \quad (2) X = V_0 t + \frac{1}{2} at^2 \quad (3) V^2 = V_0^2 + 2ax$$

Where X is displacement, V_0 is velocity at $t = 0$, V is velocity at time t, a is acceleration these are Kinematic equations of rectilinear for constant acceleration.

2. A particle moves in a straight line with uniform acceleration. Its velocity at time $t=0$ is V_1 and at time $t = t$ is V_2 . The average velocity of the particles in this time interval is $\left(\frac{V_1 + V_2}{2}\right)$. Is this correct? Substantiate your answer?

Ans:- Let us consider particle moving with uniform acceleration "a"

at $t = 0$, initial velocity = V_1

$t = t$, final velocity = V_2

time = t

From (1) eq. to $V_2 = V_1 + at$

$$\Rightarrow a = \frac{V_2 - V_1}{t}$$

and (2) eq. to $S = V_1 t + \frac{1}{2} at^2$

$$S = V_1 t + \frac{1}{2} \left(\frac{V_2 - V_1}{t} \right) \times t^2$$

$$S = t \left[V_1 + \frac{V_2 - V_1}{2} \right]$$

$$S = t \left[\frac{V_1 + V_2}{2} \right]$$

$$\frac{S}{t} = \frac{V_1 + V_2}{2}$$

∴ The given statement is correct.

3. **Can the velocity of an object be in a direction other than the direction of acceleration of the object? If so, given an example?**

Ans:- Yes, the velocity of an object can be in a direction other than the direction of acceleration of the object.

Example : In the case of the upward motion of a projectile the angle between velocity and acceleration is 180° . During its journey the direction of velocity is upwards and the direction of acceleration is downwards.

4. **A parachutist flying in an aeroplane jumps when it is at a height of 3 Km above ground. He opens his parachute when he is about 1 Km above ground. Describe his motion?**

Ans:- Consider that the aeroplane is flying horizontally. The person jumping from the aeroplane is treated as a freely falling body because his initial velocity in the vertically downward direction is zero. At a height of about 1 km the person gets a uniform velocity called terminal velocity due to air friction. Hence the acceleration becomes zero. Hence the person falls with a constant velocity straight line from 1 km onwards.

5. **A bird holds a fruit in its beak and flies parallel to the ground. It lets go of the fruit at some height. Describe the trajectory of the fruit as it falls to the ground as seen by (a) the bird (b) a person on the ground?**

Ans:- Let a horizontally flying bird drop a fruit.

1) The trajectory of the fruit with respect to the bird is a straight line.

2) The trajectory of the fruit with respect to the person on the ground is a parabola.

6. **A man runs across the roof of a tall building and jumps horizontally on the (lower) roof of an adjacent building. If his speed is u m/s and the horizontal distance between the buildings is 10m and the height difference between the roofs is 9m, will he be able to land on the next building?**

Ans:- $u = 9 \text{ m/s}$, $g = 10 \text{ m/s}^2$, $h = 9 \text{ m}$

$$\text{Range} = 4 \times t$$

$$\text{But } t = \sqrt{\frac{2h}{g}}$$

$$\begin{aligned} R &= u \cdot \sqrt{\frac{2h}{g}} = 9 \times \sqrt{\frac{2 \times 9}{10}} \\ &= 9 \times \sqrt{\frac{18}{10}} \\ &= 9 \times 1.4 \cong 12.6\text{m} \end{aligned}$$

Range is greater than distance

between two buildings

$$R > S$$

\therefore The man safely land on the next building.

7. A ball dropped from the roof of a full building and simultaneously another ball is thrown horizontally with some velocity from the same roof which ball lands first? Explain your answer?

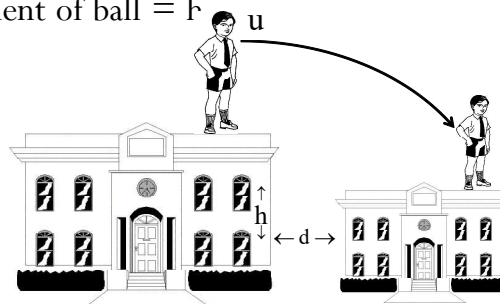
Ans:- Let height of the building = Displacement of ball = h

For first ball $u=0$, $s=h$, $a=g$, $t=t_1$

$$S = ut + \frac{1}{2} at^2$$

$$h = 0 + \frac{1}{2} gt_1^2$$

$$t_1 = \sqrt{\frac{2h}{g}} \quad \text{-----} \rightarrow (1)$$



For second ball

$u_x = u_1$, $u_y = 0$, $a_y = g$, $s_y = h$, $t = t_2$

$$s_y = u_{y1}t + \frac{1}{2} a_y t^2$$

$$h = 0 + \frac{1}{2} gt_2^2$$

$$t_2 = \sqrt{\frac{2h}{g}}$$

\therefore From eq'n. (1) & (2) are equal.

$$t_1 = t_2$$

\therefore Two balls will reach the ground in same time.

8. A ball is dropped from a building and simultaneously another ball is projected upwards with some velocity. Describe the change in relative velocities of the ball as a function of time?

Ans:- Case (i) For the 1st body

$$V_1 = u + gt$$

(or)

$$V_1 = gt \quad \text{-----(1).}$$

For the 2nd body

$$V_2 = u - gt \quad \text{-----(2)}$$

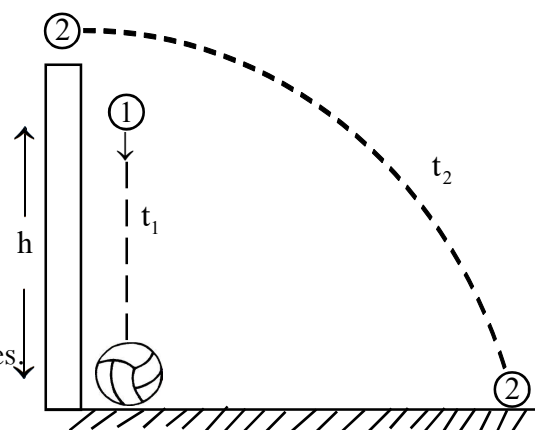
Relative velocity between (1) & (2) bodies,

$$V_2 + V_1 = u - gt + gt = u$$

$$V_2 + V_1 = u$$

The relative velocities of the body is always constant.

Hence the change in the relative velocity is zero.



9. A typical raindrop is about 4mm in diameter. If a raindrop falls from a cloud which is at 1 km above the ground, estimate its momentum when it hits the ground?

Ans:- Density of water $\rho_w = 1000 \text{ kg/m}^3$

Radius of rain drop $r = 2 \text{ mm} = 2 \times 10^{-3} \text{ m}$

Height $h = 1 \text{ km} = 10^3 \text{ m}$

$$V^2 - u^2 = 2as \quad (\text{or}) \quad V = \sqrt{2gh}$$

$$\therefore V = \sqrt{2 \times 9.8 \times 10^3} = 140 \text{ m/s}$$

$$P = MV = \frac{4}{3} \pi r^3 \rho V$$

$$= \frac{4}{3} \times 3.14 \times (2 \times 10^{-3})^3 \times 1000 \times 140$$

$$\therefore P = 0.00469 \text{ kg m/sec}$$

10. Show that the maximum height reached by a projectile launched at an angle of 45° is on quata of its range?

$$\text{Ans:- } \theta = 45^\circ \text{ Range} = \frac{4^2 \sin^2 \theta}{g} = \frac{4^2 \sin 90^\circ}{g} = \frac{4^2}{g} \text{ ----- (1)}$$

$$\text{Maximum height } H = \frac{4^2 \sin^2 \theta}{2g} = \frac{4^2 \sin^2 (45)}{2g} = \frac{1}{4} \frac{4^2}{g} \text{ ----- (2)}$$

$$\therefore \boxed{H = \frac{R}{4}}$$

Problems :

1. A bullet moving with a speed of 150 m/sec strikes a tree and penetrates 3.5cm before stopping what is the magnitude of its vetardation in the tree and the time taken for it to stop after striking the tree?

$$\text{Ans:- } u = 150 \text{ m/s } S = 3.5 \text{ cm} = 0.035, V = 0$$

$$V^2 - u^2 = 2as$$

$$0^2 - 150^2 = 2 \times 9 \times 0.035 \Rightarrow a = \left| \frac{-150 \times 150}{2 \times 0.035} \right|$$

$$a = -3.214 \times 10^5 \text{ m/s}^2$$

$$t = \frac{V - u}{a} = \frac{0 - 150}{-3.24 \times 10^5} = 4.67 \times 10^4 \text{ sec}$$

2. A food packet is ropped from an aeroplane moving with a speed of 360 Knysh in a horizontal direction, trom a hight of 500m. Find (1) its time of descent (2) the horizonatal distance between the point at which the food packet reaches the ground and the point above which it was dropped? ($g = 10 \text{ m/s}^2$)

$$\text{Ans:- } \text{Velocity of aeroplane } V = 360 \text{ knysh} = 360 \times \frac{5}{18} \text{ h} = 100 \text{ m/s}$$

$$h = 500 \text{ m}$$

$$\text{i) Time of decent} = + = \sqrt{\frac{2h}{g}} = \sqrt{\frac{2 \times 500}{10}} = 10 \text{ sec}$$

$$\text{ii) Horizontal range } R = 4 \times \sqrt{\frac{2h}{g}} = 100 \times 10 = 1000 \text{ sec}$$

3. A ball is tossed from the window of a building with an initial velocity of 8 m/s, at an angle of 20° below the horizontal. It strikes the ground 3 sec later. From what height was the ball thrown? How far from the base of the building does the ball strike the ground.

Ans:- $u = 8 \text{ m/s}$ $\theta = 20^\circ$, $t = 3 \text{ sec}$

$$\begin{aligned} \text{(a) Horizontal distance} &= u \cos \theta \times t = 8 \cos 20^\circ \times 3 \\ &= 8 \times 0.9397 \times 3 \\ &= 22.6 \text{ m} \end{aligned}$$

$$\begin{aligned} \text{(b) Height } h &= (u \sin \theta) t + \frac{1}{2} g t^2 \\ &= 8 \times \sin 20^\circ + \frac{1}{2} \times 9.8 \times 9 \\ &= 8.208 + 44.1 = 52.31 \text{ m} \end{aligned}$$



UNIT IV

MOTION IN A PLANE

VERY SHORT QUESTION & ANSWERS (2 MARKS)

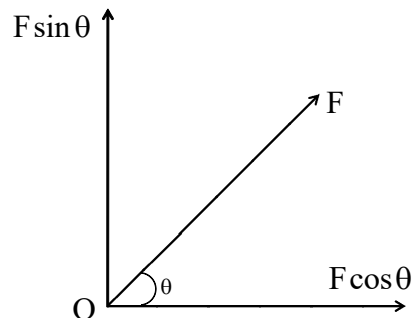
1. The vertical component of a vector is equal to its horizontal components. What is the angle made by the vector with x - axis.

Ans:- The horizontal component is equal to the vertical component of a vector

$$F \cos \theta = F \sin \theta$$

$$\tan \theta = 1 \Rightarrow \theta = \tan^{-1}(1) = 45^\circ$$

$\theta = 45^\circ$



2. A vector V makes an angle with the horizontal. The vector is rotated through an angle \hat{e} . Does this rotation change the vector V ?

Ans:- Yes it changes the vector.

3. Two forces of magnitude 3 units and 5 units act at 60° with each other. What is the magnitude of their resultant?

Ans:- $P = 3$ unit $Q = 5$ unit $\theta = 60^\circ$

$$\begin{aligned} R &= \sqrt{P^2 + Q^2 + 2PQ \cos \theta} = \sqrt{3^2 + 5^2 + 2 \times 3 \times 5 \times \frac{1}{2}} \\ &= \sqrt{9 + 25 + 15} \\ &= \sqrt{49} \\ &= 7 \text{ units} \end{aligned}$$

4. $\vec{A} = \vec{i} + \vec{j}$ what is the angle between the vector and x - axis?

Ans:- $\vec{A} = \vec{i} + \vec{j}$

$$\begin{aligned} \cos \alpha &= \frac{A_x}{|A|} \quad (\because A_x = 1) \\ &= \frac{1}{\sqrt{1^2 + 1^2}} = \frac{1}{\sqrt{2}} \\ \alpha &= \cos^{-1} \left(\frac{1}{\sqrt{2}} \right) = 45^\circ \end{aligned}$$

$\alpha = 45^\circ$

5. When two right angled vectors of magnitude 7 units and 24 units combine, what is the magnitude of their resultant?

Ans:- $\theta = 90^\circ$, $P = 7$ units, $Q = 24$ units

$$\begin{aligned} R &= \sqrt{P^2 + Q^2 + 2PQ \cos \theta} = \sqrt{7^2 + 24^2 + 2 \times 7 \times 24 \times 0} \\ &= \sqrt{49 + 576 + 0} \\ &= \sqrt{625} \\ &= 25 \text{ units.} \end{aligned}$$

6. If $P = 2i + 4j + 14k$, and $Q = 4i + 4j + 10k$ find the magnitude of $P + Q$

Ans:- $P = 2i + 4j + 14k$, $Q = 4i + 4j + 10k$

$$\vec{P} + \vec{Q} = 2i + 4j + 14k + 4i + 4j + 10k = 6i + 8j + 24k$$

$$\begin{aligned} |\vec{P} + \vec{Q}| &= \sqrt{6^2 + 8^2 + 24^2} = \sqrt{36 + 64 + 576} = \sqrt{676} \\ &= 26 \end{aligned}$$

7. Can a vector of magnitude zero have non zero components?

Ans:- No, the components of a vector of magnitude zero have non-zero components.

8. What is the acceleration of projectile at the top of its trajectory.

Ans:- The acceleration of a projectile at the top of its trajectory is vertically downwards.

9. Can two vectors of unequal magnitude add up to give the zero vector? Can three unequal vectors add up to give the zero vector?

Ans:- No, two vectors of unequal magnitude cannot be equal to zero. According to triangle law, three unequal vectors in equilibrium can be zero.

SHORT QUESTION & ANSWERS (4MARKS)

1. State parallelogram law of vectors. Derive an expressions for the magnitude and direction of the resultant vectors?

Ans:- Statement : If two vectors acting at a point are represented by the adjacent sides of a parallelogram in magnitude and direction then their resultant is represented by the diagonal of the parallelogram in magnitude and direction drawn from the same point.

Explanation :

$$\vec{OA} = \vec{BC} = \vec{P}$$

$$\vec{OB} = \vec{AC} = \vec{Q}$$

$$\vec{OC} = \vec{R}$$

Resultant magnitude : From ΔCOD

$$OC^2 = OD^2 + CD^2$$

$$OC^2 = (OA + AD)^2 + CD^2$$

$$OC^2 = OA^2 + AD^2 + 2OA \cdot AD + CD^2$$

$$\text{But } \Delta CAD \Rightarrow AD^2 + CD^2 = AC^2$$

$$\Rightarrow OC^2 = OA^2 + AC^2 + 2OA \cdot AD \text{ -----} \rightarrow (1)$$

$$\text{From } \Delta CAD \cos \theta = \frac{AD}{AC}$$

$$AD = Q \cos \theta \text{ -----} (2)$$

$$\Delta CAD \sin \theta = \frac{CD}{AC}$$

$$CD = Q \sin \theta \text{ ----} (3)$$

(2) eqn substitute in (1) eqn

$$R^2 = P^2 + Q^2 + 2P \cdot Q \cos \theta$$

$$R = \sqrt{P^2 + Q^2 + 2PQ \cos \theta}$$

$$\text{Resultant Direction : } \tan \alpha = \frac{CD}{OD}$$

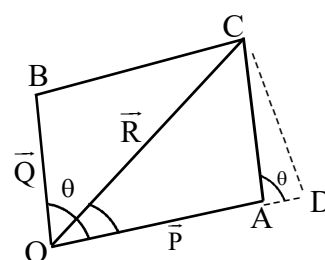
$$\tan \alpha = \frac{CD}{OA + AD}$$

From (2) & (3) eq.n to

$$\tan \alpha = \frac{Q \sin \theta}{OA + Q \cos \theta}$$

$$\tan \alpha = \frac{Q \sin \theta}{P + Q \cos \theta}$$

$$\alpha = \tan^{-1} \left(\frac{Q \sin \theta}{P + Q \cos \theta} \right)$$



2. What is relative motion? Explain it?

Ans:- **Relative Motions** : The motion of body with respect to another body is called the relative motion. The corresponding velocity is called the relative velocity.

Explanaion : Let us consider two persons A & B moving with velocities \vec{V}_A and \vec{V}_B in two different directions making an angle with each other.

1) The relative velocity of body A with respect to B is given by $\vec{V}_R = \vec{V}_A - \vec{V}_B$

- 2) The relative velocity of body B with respect to A is given by $\vec{V}_R = \vec{V}_B - \vec{V}_A$
- 3) \vec{V}_R , \vec{V}_R are equal magnitudes and opposite in directions.
- 4) $|\vec{V}_R| = |\vec{V}_A - \vec{V}_B| = \sqrt{V_A^2 + V_B^2 - 2 V_A V_B \cos \theta}$
- 5) For two bodies moving in the same directions relative velocity is equal to the difference of velocities ($\theta = 0^\circ$, $\cos 0^\circ = 1$) $\Rightarrow |\vec{V}_R| = |\vec{V}_A - \vec{V}_B|$
- 6) For two bodies moving in the opposite directions relative velocity is equal to the sum of their velocity ($\theta = 180^\circ$, $\cos 180^\circ = -1$)
- $$\Rightarrow |\vec{V}_R| = \vec{V}_A + \vec{V}_B$$
- 7) If they move at right angle to each other then the relative velocity = $\sqrt{V_1^2 + V_2^2}$
- 8) If $\vec{V}_A = \vec{V}_B = V$ then $V_{rel} = 2V \sin \frac{\theta}{2}$

3. Show that a boat must move at angle with respect to given water in order to cross the river in minimum time?

Ans:- The boat is directed making an angle " θ " with direction of water current. The angle between \vec{V}_b and \vec{V}_w as shown in fig.

→ The component of \vec{V}_b across the river is given as $V_{by} = V_b \sin \theta$

→ When the boat reaches the other bank displacement of boat = width of the river = d

$$\text{Time taken to cross the river} = \frac{\text{Displacement of boat across the river}}{\text{Component of velocity of boat across the river}}$$

$$t = \frac{d}{V_{by}} = \frac{d}{V_b \sin \theta}$$

When θ is maximum then time becomes minimum.

$$\sin \theta = 1 \Rightarrow \theta = 90^\circ$$

$$\therefore \text{Minimum time taken to cross the river, } t = \frac{d}{V_b}$$

4. Define unit vector, null vector and position vector?

Ans:- Unit vector : A vector having unit magnitude is called unit vector.

$$\hat{A} = \frac{A}{(A)} \text{ where } \hat{A} \text{ is unit vector.}$$

Null vector : A vector having zero magnitude is called null vector.

Position vectors : The position of a particle is described by a position vector which is drawn from the origin of a reference frame. The position vector helps to locate the particle in space.

$$\vec{OP} = \vec{r} = \vec{x}\hat{i} + \vec{y}\hat{j} + \vec{z}\hat{k}$$

5. If $|\vec{a} + \vec{b}| = |\vec{a} - \vec{b}|$ prove that the angle between \vec{a} and \vec{b} is 90° .

Ans:- $|\vec{a} + \vec{b}| = \sqrt{a^2 + b^2 + 2ab\cos\theta}$

$$|\vec{a} - \vec{b}| = \sqrt{a^2 + b^2 - 2ab\cos\theta}$$

$$\therefore |\vec{a} + \vec{b}| = |\vec{a} - \vec{b}|$$

$$\sqrt{a^2 + b^2 + 2ab\cos\theta} = \sqrt{a^2 + b^2 - 2ab\cos\theta}$$

$$2ab\cos\theta = -2ab\cos\theta$$

$$4ab\cos\theta = 0$$

$$\cos\theta = 0 \text{ but } 4ab \neq 0$$

$$\theta = 90^\circ$$

Hence angle between \vec{a} and \vec{b} is 90° .

6. Show that the trajectory of an object thrown at an angle with the horizontal is a parabola.

Ans:- Consider a body is projected with an initial velocity (u) making an angle θ with the horizontal. The velocity of the projectile, x-direction $u\cos\theta$ and y-direction $u\sin\theta$.

The distance travelled along ox in time 't' is given by

$$x = u\cos\theta \times t$$

$$t = \frac{x}{u\cos\theta} \quad \text{----- (1)}$$

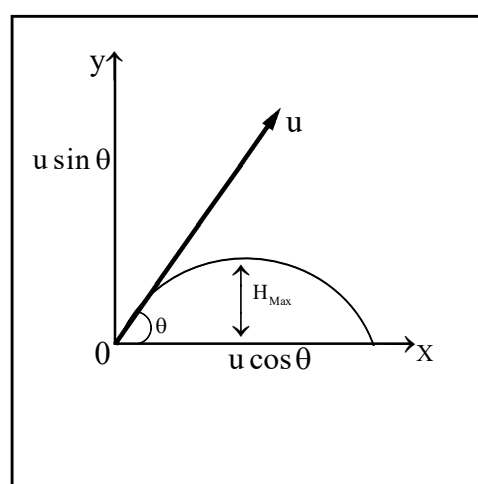
along with y - direction in time 't' is given by

$$y = u\sin\theta \times t + \frac{1}{2}(-g) \times t^2$$

but (1) eq'n $t = \frac{x}{u\cos\theta}$ then

$$y = u\sin\theta \left(\frac{x}{u\cos\theta} \right) - \frac{1}{2}g \left(\frac{x^2}{u^2\cos^2\theta} \right)$$

$$= \tan\theta \times x - \left(\frac{g}{2u^2\cos^2\theta} \right) x^2 \quad \text{Let } A = \tan\theta$$



$$y = Ax - Bx^2 \quad B = \frac{g}{2u^2 \cos^2 \theta}$$

This is the equation of parabola.

\therefore The trajectory of a projectile is parabola.

7. Explain the terms the average velocity and instantaneous velocity. When are they equal?

Ans:- **Average Velocity** : The average velocity of the particles is defined as the ratio of displacement (Δx) to the time interval Δt

$$\therefore \bar{V} = \frac{\Delta x}{\Delta t} = \frac{x_2 - x_1}{t_2 - t_1}$$

Instantaneous velocity : A velocity of the particle at any instant of time is called instantaneous velocity.

$$V_{\text{Insta}} = \lim_{\Delta t \rightarrow 0} \frac{\Delta x}{\Delta t} = \frac{ds}{dt}$$

For a body moving with uniform velocity its average velocity is equal to the instantaneous velocity.

8. Show that the maximum height and range of a projectile are $\frac{u^2 \sin^2 \theta}{2g}$ and $\frac{u^2 \sin 2\theta}{g}$ respectively where the terms have their regular meanings.

Ans:- **Maximum height** : when the projectile is at the maximum height, its vertical component of velocity $V_y = 0$.

initial velocity (u) = $u \sin \theta$

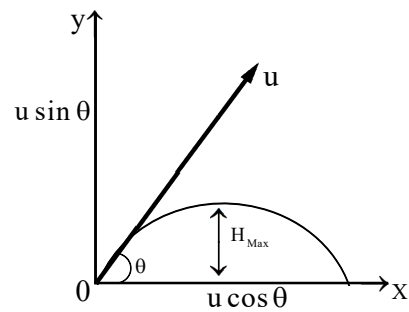
$S = H = \text{maximum height}$

$a = -g$

$$V^2 - u^2 = 2as$$

$$0 - u^2 \sin^2 \theta = -2gH$$

$$\boxed{H = \frac{u^2 \sin^2 \theta}{2g}}$$



Horizontal ranges (R) : The horizontal distance travelled by the projectile from the point of projection during the time of flight is called range.

Range (R) = Horizontal velocity x time

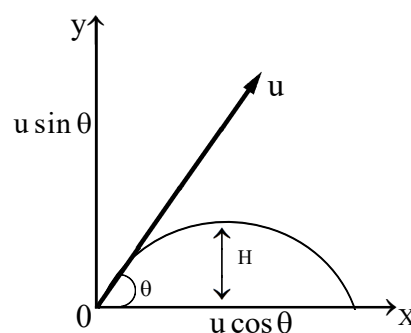
$$R = u \cos \theta \times t = u \cos \theta \times \frac{2u \sin \theta}{g}$$

$$= \frac{u^2 2 \sin \theta \cos \theta}{g}$$

$$R = \frac{u^2 \sin 2\theta}{g}$$

if $\theta = 45^\circ$

$$R_{\max} = \frac{u^2}{g}$$



9. If the trajectory of a body is parabolic in one reference frame, can it be parabolic in another reference frame that moves at constant velocity with respect to the first reference frame? If the trajectory can be other than parabolic what else can it be?

Ans:- No, when a stone is thrown from a moving bus, the trajectory of the stone is parabolic in one reference frame. That is when a man observes outside footpath. In another frame of reference the trajectory is a vertical straight line.

10. A force $2\mathbf{i} + \mathbf{j} - \mathbf{k}$ newton acts on a body which is initially at rest. At time ends of 20 sec. The velocity of the body is $4\mathbf{i} + 2\mathbf{j} - 2\mathbf{k}$ m/s what is the mass of the body?

Ans:- $F = (2\mathbf{i} + \mathbf{j} + \mathbf{k})\text{N}$ $t = 20$ sec, $u = 0$, $V = 4\mathbf{i} + 2\mathbf{j} - 2\mathbf{k}$

$$a = \frac{V - u}{t} = \frac{4\mathbf{i} + 2\mathbf{j} - 2\mathbf{k}}{20} = \frac{2(2\mathbf{i} + \mathbf{j} - \mathbf{k})}{2 \times 10} = \frac{2\mathbf{i} + \mathbf{j} - \mathbf{k}}{10} \text{ m/sec}$$

$$\text{But } F = ma \Rightarrow m = \frac{F}{a} = \frac{2\mathbf{i} + \mathbf{j} - \mathbf{k}}{\frac{2\mathbf{i} + \mathbf{j} - \mathbf{k}}{10}}$$

$$m = 10 \text{ kg}$$

Problems :

1. A projectile is fired at an angle of 60° to the horizontal with an initial velocity of 800m/s
 - i) Find the time of flight of the projectile before it hits the ground.
 - ii) Find the distance it travels before it hits the ground (Range)
 - iii) Find the time of flight for the projectile to reach its maximum height.

Sol:- $\theta = 60^\circ$, $u = 800$ m/sec

$$\begin{aligned} \text{i) } T &= \frac{2u \sin \theta}{g} = \frac{2 \times 800 \times \sin 60^\circ}{9.8} \\ &= \frac{2 \times 800 \times \sqrt{3}}{9.8 \times 2} \end{aligned}$$

$$T = 141.4 \text{ sec}$$

$$(ii) \text{ Range} = \frac{u^2 \sin 2\theta}{g} = \frac{(800)^2 \times \sqrt{3}}{9.8 \times 2} = 56.57 \text{ km}$$

$$iii) t_a = \frac{u \sin \theta}{g} = \frac{800 \times \sin 60^\circ}{9.8} = \frac{800 \times \sqrt{3}}{9.8 \times 2}$$

$$t_a = 70.7 \text{ sec}$$

2. For a particle projected slantwise from the ground, the magnitude of its position vector with respect to the point of projection, when it is the highest point of the path is found to be $\sqrt{2}$ times the maximum height reached it show that the angle of projection is $\tan^{-1}(2)$.

Sol:- $\text{Range (R)} = \frac{u^2 \sin 2\theta}{g}, H_{\max} = \frac{u^2 \sin^2 \theta}{2g}$

Give $R = \sqrt{2} H$

$$\frac{u^2 \sin \theta \cos \theta}{g} = \sqrt{2} \frac{u^2 \sin^2 \theta}{2g}$$

$$\tan \theta = 2\sqrt{2}$$

$$\boxed{\theta = \tan^{-1}(2\sqrt{2})}$$

3. An object is launched from a cliff 20m above the ground at an angle of 30° above the horizontal with an initial speed of 30m/s. How horizontally does the object travel before landing on the ground? ($g = 10 \text{ m/s}^2$)

Sol:- $h = 20\text{m}, \theta = 30^\circ, u = 30 \text{ m/s}, g = 10 \text{ m/s}^2$

$$h = -(u \sin \theta)t + \frac{1}{2}gt^2$$

$$20 = -30 \sin 30^\circ \times t + \frac{1}{2} \times 10t^2$$

$$20 = -30 \times \frac{1}{2} \times t + \frac{1}{2} 10t^2$$

$$4 = -3t + t^2$$

$$t^2 - 3t - 4 = 0$$

$$(t-4)(t+1) = 0$$

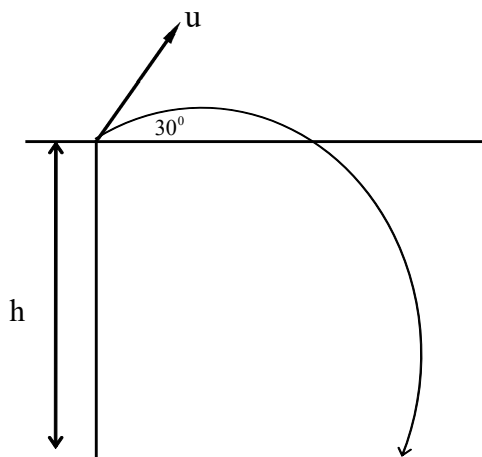
$$t = 4\text{sec (or)} t = -1 \text{ sec}$$

$$\text{Range } R = u \cos \theta \times t$$

$$= 30 \cos 30^\circ \times 4$$

$$= 30 \times \frac{\sqrt{3}}{2} \times 4$$

$$\boxed{R = 60\sqrt{3} \text{ m}}$$



4. A particle is projected from the ground with some initial velocity making an angle of 45° with the horizontal. It reaches a height of 7.5m above the ground while it travels a horizontal distance of 10m from the point of projection. Find the initial speed of projection. ($g=10\text{m/s}^2$)

Ans:- $\theta = 45^\circ$, $g = 10\text{m/s}^2$ Hd (x) = 10
Yd (y) = 7.5m

$$y = \tan \theta x - \frac{g}{2u^2 \cos^2 \theta} x^2$$

$$7.5 = \tan 45^\circ \times 10 - \frac{10}{2u^2 \cos^2 45^\circ} \times 10^2$$

$$7.5 = 10 - \frac{1000}{2u^2 \times \frac{1}{2}}$$

$$\frac{1000}{u^2} = 2.5 \Rightarrow u^2 = \frac{1000}{2.5}$$

$$u^2 = 400$$

$$\boxed{u = 20 \text{ m/s}}$$



LAWS OF MOTION

VERY SHORT QUESTION & ANSWERS (2 MARKS)

3. When a bullet is fired from a gun, the gun gives a kick in the backward direction? Explain?

Ans:- According to law of conservation of momentum when a bullet is fired from a gun, the momentum of the gun is equal and opposite to that of bullet. As the bullet moves forward on firing, the gun moves back.

4. Why does a heavy rifle not recoil as strongly as a light rifle using the same cartridges?

Ans:- As the mass of the rifle is more its acceleration is less. Therefore, a heavy rifle doesn't recoil as strongly as a light rifle.

5. If a bomb at rest explodes in two pieces the pieces must travel in opposite direction. Explain?

Ans:- According to law of conservation of momentum.

$$Mu = m_1u_1 + m_2u_2$$

initially $u = 0$

$$m_1u_1 + m_2u_2 = 0 \quad \text{or} \quad m_1v_1 = m_2v_2$$

(-ve sign indicates that the pieces must travel in opposite direction)

6. Define force. What are the basic forces in nature?

Ans:- It is that which changes or tries to change the state of body.

Basic forces : 1) Gravitational forces 2) Electromagnetic forces

3) Strong nuclear forces 4) weak nuclear

7. Can the coefficient of friction be greater than one?

Ans:- Yes, coefficient of friction may be greater than one. In some particular cases it is possible. They are

1) Due to increase the inner molecular attractive forces between surfaces when the contact surfaces are highly polished.

2) When the contact surfaces of the bodies are interlocking the coefficient of friction may be greater than one.

8. **Why does the car with a flatened tyre stop sooner than the one with inflated tyres?**

Ans:- In case of flatened tyres more deformation occurs. when compared to that of inflated tyres. Since rolling friction is directly proportional to the area of contact. Flatened tyres stop sooner than of inflated tyres.

9. **A horse has to pull harder during the starts of the motion than later. Explain?**

Ans:- Initially the cart has to overcome the limiting friction. Once motion has started the frictional forces decrease. Hence the horse has to pull cart harder during start.

10. **What happens to the coefficient of friction if the weight of the body is doubled?**

Ans:- Coefficient of friction is independent of mass of the body. Hence it remains.

SHORT QUESTION & ANSWERS (4MARKS)

1. **A stone of mass 0.1kg is thrown vertically up ward. Give the magnitude and direction of the net force on the stone (a) during its upward motion (b) during its downward motion, (c) at the highest point, where it momentarily comes to rest.**

Ans:- (a) during upward motion : Magnitude of the net force of the stone.

$$F = |-mg| : = 0.1 \times 9.8 = 0.98\text{N}$$

(b) During downward motion : Magnitude of the net force of the stone.

$$F = |-mg| : = 0.1 \times 9.8 = 0.98\text{N}$$

(c) At the highest point : Magnitude of the net force

$$F = mg = 0.1 \times 9.8 = 0.98\text{N}$$

4. **Explain the terms limiting friction, dynamic friction and rolling friction.**

Ans:- **Limiting friction** : The maximum frictional force developed between the bodies at rest is called limiting friction.

Dynamic friction : Frictional force between bodies in motion is called dynamic (or) kinetic friction.

Rolling friction : When one body rolls on the surface of the other body, then the friction in between the surfaces is called rolling friction.

5. **Explain advantages and disadvantages of friction?**

Ans:- **Advantages of friction** :

1) Walking on the floor, motion of vehicles etc. are possible only due to friction.

- 2) Nails, screws etc. are driven into walls, wooden surfaces etc. due to friction.
- 3) Writing with pens, pencils, holding objects with hands etc, is possible due to friction.
- 4) A match stick is lightened due to friction.

Disadvantages of friction :

- 1) Wear and tear of machine parts are due to friction.
- 2) Energy is wasted as heat due to friction.

6. Mention the methods used to decrease friction?

Ans:- Methods to reduce friction.

- (a) **Polishing** : Polishing the surfaces in contact decreases the interlocking and thereby friction can be reduced.
- (b) **Ball bearings** : Ball bearings can reduce the friction since rolling friction is less than the sliding friction.
- (c) **Lubricants** : Lubricants like grease form a thin layer between surfaces in contact. It reduces the friction.
- (d) **Streamlining** : Automobiles and aeroplanes are streamlined to reduce the air friction.

7. State the laws of rolling friction?

Ans:- Laws of friction - rolling friction :

- 1) The smaller the area of contact, the lesser will be the rolling friction.
- 2) The larger the radius of the rolling body the lesser will be the rolling friction.
- 3) The rolling friction is directly proportional to the normal reaction.

If F_r is the rolling friction and "N" is the normal reaction at the contact then

$$F_r \propto N.$$

$$\Rightarrow F_r = \mu_r N \quad \text{Where } \mu_r \text{ is the coefficient of rolling friction.}$$

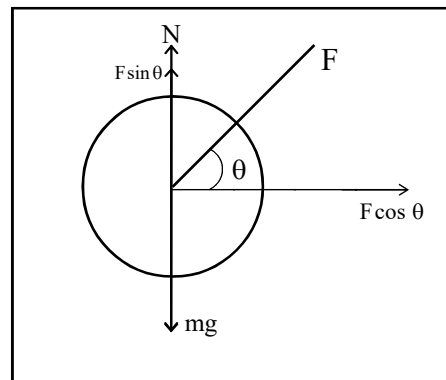
8. Why is pulling the lawn roller preferred in pushing it?

Ans:- **Pulling** : Consider a lawn roller of weight mg acting on the horizontal surface. It is pulled by a force F making an angle θ with horizontal. The force F can be resolved into two components (i) $F \cos \theta$, horizontally along the road and (ii) $F \sin \theta$, vertically upwards.

Total upward force = Total downward force

$$N + F \sin \theta = mg$$

$$N = mg - F \sin \theta$$



The frictional force $f_r = \mu_r \cdot N$

$$f_r = \mu_r [mg - F \sin \theta]$$

The net force on the pulling of roller $P = F \cos \theta - f_r$.

$$P = F[\cos \theta + \mu_r \sin \theta] - \mu_r mg \quad \text{----- (1)}$$

Pushing : when a lawn roller is pushed by a force.

F which makes an angle θ with the horizontal, $F \sin \theta$ acts vertically down ward and $F \cos \theta$ pushes the roller to the right. The weight mg acts vertically down wards.

$$N = mg + F \sin \theta$$

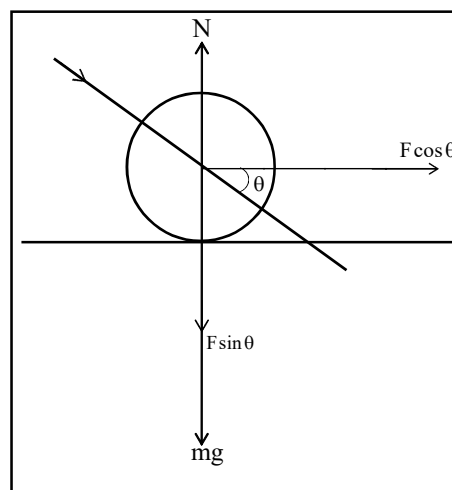
The frictional force (f_r) = $\mu_r N$

$$= \mu_r (mg + F \sin \theta)$$

The net force on the pushing of roller $P = F \cos \theta - f_r$.

$$P = F[\cos \theta - \mu_r \sin \theta] - \mu_r mg \quad \text{----- (2)}$$

From equation (1) and (2) that it is easier to pull than push a lawn roller.



1. A boy is moving along a circular path such that its speed always remains constant. Should there be a force acting on the body?

Ans:- **Force on a body moving in a circular path :** Due to the change in direction of velocity in circular path the body experiences centripetal force, even though magnitude of velocity always remains constant.

Problems :

1. The linear momentum of a particle as a function of time t is given by $p = a + bt$, where a and b are positive constants, what is the force acting on the particle?

Ans:- Linear momentum of a particle $P = a + bt$

$$\text{Force } F = \frac{dp}{dt} = \frac{d}{dt} (a + bt) = 0 + b \quad \boxed{F = b}$$

2. Calculate the time needed for a net force of 5N to change the velocity of a 10 Kg mass by m/sec^2

Ans:- $F = 5N$, $m = 10Kg$ $(v - u) = 2m/sec$ $t = ?$

$$F = m \frac{(v - u)}{t} \Rightarrow 5 = \frac{10(2)}{t} = 4sec$$

$$\boxed{t = 4 \text{ sec}}$$

3. A constant force acting on a body of mass 3Kg changes its speed from 2 in m/sec to 3.5 m/s in 25 sec, The direction of motion of the body reamaing unchanged. What is the magnitude and aircetion of the force.

Ans:- $m = 3\text{kg}$ $u=2\text{m/sec}$ $v=3.5\text{m/sec}$, $t=25\text{sec}$.

$$F = m \left(\frac{v - u}{t} \right) = \frac{3 (1.5)}{25} = \frac{4.5}{25} = 0.18\text{N}$$

4. A container of mass 200 kg rests on the back of an open trusk. If the truck accelerates at 1.5 m/s² what is the minimum cafficient of static, friction between the container and the bed of the truck reguired to prevent the container from sliding of the back of the truck?

Ans:- $m = 200\text{Kg}$ $a=1.5 \text{ m/s}^2$ $g=9.8\text{m/s}^2$

$$F = \mu_s \cdot N \quad N = mg$$

$$ma = \mu_s \cdot mg \quad F = ma$$

$$\mu_s = \frac{9}{8} = \frac{1.5}{9.8} = 0.153$$



UNIT VI

WORK, ENERGY AND POWER

VERY SHORT QUESTION & ANSWERS (2 MARKS)

1. State the condition under which a force does no work?

- Ans:- 1) When the displacement is zero.
2) When the displacement is perpendicular to the direction of the force.
3) When the body moves under the action of a conservative force over a closed path.

2. Define, work, power and Energy. State their S.I units?

- Ans:- Work : The product of magnitude of displacement and component of force along the direction of displacement is called work.

$$W = \vec{F} \cdot \vec{S} = F.S \cos \theta$$

Unit : Joyle.

Power : The rate of doing work by a force is called power.

$$P = \frac{W}{t} \quad \text{Units : Watt or J/sec}$$

Energy : The capality to do work is called energy.

Unit : Joyle.

3. State the relation between the kinetic energy and momentum of a body?

Ans:- Kinetic energy $E_k = \frac{p^2}{2m}$

P = momentum of the body

m = mass of the body.

4. State the sign of work done by a force in the following

(a) Work done by a man in lifting a bucket out of a well by means of rope tied to the bucket.

(b) Work done gravitational force in the above case.

- Ans:- (a) Work done is +Ve, because the bucket displaces in the direction of force.

(b) Work done is -Ve, because the displacement is opposite to the gravitational force.

$$W = F.S \cos \theta = F.S \cos 180^\circ = - F.S$$

5. State the sign of work done by a force in the following.

(a) Work done by friction on a body sliding down an inclined plane.

(b) Work done by gravitational force in the above case?

Ans:- (a) Work done is -Ve, because friction always opposite to the direction of the motion.

(b) The work done is +Ve.

6. State the sign of work done by a force in the following.

(a) Work done by an applied force on a body moving on a rough horizontal place with uniform velocity.

(b) Work done by the resistive force of air on a vibrating pendulum in bringing it to rest?

Ans:- (a) The work done is +Ve, because the applied force and displacement are in the same direction.

(b) The work done is -Ve, because the direction of resistive force is opposite to the direction of motion of the pendulum.

7. State if each of the following statement is true or false. Give reasons for your answer, (a) Total energy of a system is always conserved, no matter what internal and external forces on the body are present.

(b) The work done by earth's gravitational force in keeping the moon in its orbit one revolution is zero.

Ans:- a) False b) True. Because gravitational force is conservative force.

8. Which physical quantity remains constant.

i) in an elastic collision ii) in an inelastic collision.

Ans:- i) in elastic collision : Both momentum and kinetic energy is constant.

ii) in an inelastic collision : Only momentum remains constant.

9. A body freely falling from a certain height "h" after striking a smooth floor rebounds and rises to height h/2 what is the coefficient of restitution between the floor and the body?

Ans:- Given $h_1 = h$, $h_2 = \frac{h}{2}$

$$\therefore e = \sqrt{\frac{h_2}{h_1}} = \sqrt{\frac{\frac{h}{2}}{h}} = \frac{1}{\sqrt{2}} = 0.707$$

10. What is the total displacement of a freely falling body after successive rebounds from the place of ground before it comes to stop? Assume that "e" is the coefficient of restitution between the body and the ground?

Ans:- The total displacement of the freely falling body after successive rebounds from the ground before it comes to stop is "h".

SHORT QUESTION & ANSWERS (4MARKS)

1. **What is potential energy? Derive an expression for the gravitational potential energy?**

Ans:- **Potential energy** : The energy possessed by a body by virtue of its position is called potential energy.

Examples : i) A stretched rubber cord

ii) The stone lifted above the ground.

Expression for potential energy :

A body of mass m is on the ground. It is lifted vertically upwards through a height h .

Gravitational force on the body $F = mg$

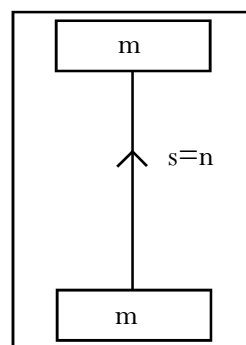
Displacement = h

Work done = $W = F \cdot S$

$$W = mgh$$

This work done is stored in the form of potential energy.

$$\boxed{P. E (U) = mgh}$$



2. **A Lorry and a Car moving with the same momentum are brought to rest by the application of brakes, which provide equal retarding forces. Which of them will come to rest in shorter time? Which will come to rest in less distance?**

Ans:- Given momentum of the lorry = momentum of the car.

$$P_L = P_C$$

and same retarding force $F_L = F_C$

$$\text{From Newton's second law } F = \frac{m(v-u)}{t} = \frac{\Delta P}{t}$$

$$W = F \cdot S = \text{change in K.E} = \frac{p^2}{2m}$$

\therefore Both lorry and car come to rest at the same time.

$$F \cdot S = \frac{p^2}{2m} \quad (\text{Here } F, p \text{ are constant})$$

$$S \propto \frac{1}{m}$$

Hence lorry comes to rest in less distance.

3. Distinguish between conservative and non-conservative forces with one example each?

Ans:- **Conservative Forces :** A force is conservative if the work done by the force on a body along any closed path is zero.

Example : Gravitational force. Work done independent of the path.

Non-conservative force : A force is called non-conservative force, is the work done by the force on a body along a closed path is not zero.

Example : Frictional force work done depends on the path.

4. Show that in the case of one dimensional elastic collision the relative velocity of approach of two colliding bodies before collision is equal to the relative velocity of separation after collision?

Ans:- Consider two bodies of masses m_1 and m_2 moving with velocities u_1 and u_2 collides elastically. Assume $m_1 > m_2$ and $u_1 > u_2$. Let v_1 and v_2 velocities of the two bodies after collision.

From the law of conservation of linear momentum

$$m_1 u_1 + m_2 u_2 = m_1 v_1 + m_2 v_2$$

$$m_1(u_1 - v_1) = m_2(v_2 - u_2) \quad \text{-----(1)}$$

From the law of conservation of kinetic energy.

$$\frac{1}{2} m_1 u_1^2 + \frac{1}{2} m_2 u_2^2 = \frac{1}{2} m_1 v_1^2 + \frac{1}{2} m_2 v_2^2$$

$$m_1(u_1^2 - v_1^2) = m_2(v_2^2 - u_2^2) \quad \text{-----(2)}$$

equation 2/1 then we get

$$u_1 + v_1 = v_2 + u_2$$

$$u_1 - u_2 = v_2 - v_1 \quad \text{-----(3)}$$

Relative velocity of approach from the above equation before collision = Relative velocity of separation after collision.

5. Show that two equal masses undergo oblique elastic collision will move at right angles after collision, if the second body initially at rest.

Ans:- **Oblique elastic collision :** If the center of mass of the colliding bodies are not initially moving along the line of impact then the impact is called oblique collision.

Two equal masses undergo oblique elastic collision will move at right angles after collision, if the second body initially at rest.

Consider two smooth and perfectly elastic spheres of masses m_1 and m_2 . Let u_1 and u_2 be their initial velocity before collision. Let v_1 and v_2 be their final velocities after collision (α, β) and (θ, ϕ) are the angles, the direction of motion make with the line of impact before collision and after collision.

$$v_1 \sin \theta = v_2 \sin \alpha \quad \text{-----(1)}$$

$$\text{and } v_2 \sin \phi = u_2 \sin \beta \quad \text{-----(2)}$$

From the conservation of momentum and kinetic energy to.

$$\therefore m_1 u_1 \cos \alpha + m_2 u_2 \cos \beta = m_1 v_1 \cos \theta + m_2 v_2 \cos \phi$$

$$\Rightarrow m_1 (u_1 \cos \alpha - v_1 \cos \theta) = m_2 (v_2 \cos \phi - u_2 \cos \beta) \quad \text{-----(3)}$$

$$\text{and } \frac{1}{2} m_1 u_1^2 \cos^2 \alpha + \frac{1}{2} m_2 u_2^2 \cos^2 \beta = \frac{1}{2} m_1 v_1^2 \cos^2 \theta + \frac{1}{2} m_2 v_2^2 \cos^2 \phi$$

$$\Rightarrow m_1 (u_1^2 \cos^2 \alpha - v_1^2 \cos^2 \theta) = m_2 (v_2^2 \cos^2 \phi - u_2^2 \cos^2 \beta) \quad \text{-----(4)}$$

equation 4/3 we will get

$$\frac{4}{3} \Rightarrow (u_1 \cos \alpha + v_1 \cos \theta) = (v_2 \cos \phi + u_2 \cos \beta).$$

$$v_1 \cos \theta = v_2 \cos \phi + u_2 \cos \beta - u_1 \cos \alpha \quad \text{-----(5)}$$

$$\text{and } v_2 \cos \phi = v_1 \cos \theta + u_1 \cos \alpha - u_2 \cos \beta \quad \text{-----(6)}$$

sub. equation (5) in equation (3) we get

$$v_1 \cos \theta = \left(\frac{m_1 - m_2}{m_1 + m_2} \right) u_1 \cos \alpha + \frac{2m_1 u_2}{m_1 + m_2} \cos \beta \quad \text{-----(7)}$$

$$\text{and } v_2 \cos \phi = \frac{2m_1 u_1}{m_1 + m_2} \cos \alpha + \left(\frac{m_1 - m_2}{m_1 + m_2} \right) u_2 \cos \beta \quad \text{-----(8)}$$

If $u_2 = 0$ and $m_1 = m_2$ then equation (2) we get $\phi = 0$ and from equation (7), $\theta = 90^\circ$. This means that if a sphere of mass "m" collides obliquely on another perfectly elastic sphere of the same mass at rest. The directions of motions of the sphere after impact will be at right angles.

6. Derive an expression for the height attained by a freely falling body after "n" number of rebounds from the floor?

Ans:- Let a sphere is dropped freely from a height "h" on to the floor. It strikes the floor with a velocity u_1 so that $u_1 = \sqrt{2gh_1}$ -----(1)

Let v_1 be the final velocity of the sphere with which the sphere rebounds to a height h_1 and

$$v_1 = \sqrt{2gh_1} \text{ since the initial and the final velocities of the floor are zero}$$

$$u_2 = 0, \quad v_2 = 0$$

$$\text{Co-efficient of restitution } e = \frac{v_2 - v_1}{u_1 - u_2} = \frac{0 - (-\sqrt{2gh_1})}{\sqrt{2gh} - 0}$$

$$e = \sqrt{\frac{2gh_1}{2gh}}$$

$$e = \sqrt{\frac{h_1}{h}} \quad (\text{or}) \quad h_1 = e^2 h$$

Similarly for the second bounce $h_2(e^2)^2 h$ and "h" bounce $\boxed{h_n = (e^2)^n h}$

7. Explain the law of conservation of energy?

Ans:- **Law of conservaton energy** : Energy can be neither created nor destroyed one form of energy can be converted into another form.

Explanation : The total mechanical energy is constant if the forces are conservative. If some of the forces are non-conservative a part of mechanical energy may be converted into another forms like sound, heat etc. But the sum of all kinds of energies is constant for the system.

The energy of the universe as a whole is constant. If one part of the universe loses energy another part must gain an equal amount of energy.

LONG QUESTION & ANSWERS (8MARKS)

1. Develop the notions of work and kinetic energy and show that it leads to work - energy theorem?

Ans:- **Kinetic energy** : Kinetic energy of a body is a measure of work done by it by virtue of its motion.

$$\therefore K_f - K_i = W$$

Proof : Consider a particle of mass "m" is moving with initial speed "u" to final speed "v". Let "a" be its constant acceleration and s be its distance traversed. The kinematic relation given by.

$$v^2 - u^2 = 2as \quad \text{---(1)}$$

multiplying both sides by $\frac{m}{2}$ we have to get

$$\frac{1}{2}mv^2 - \frac{1}{2}mu^2 = mas$$

$$\frac{1}{2}mv^2 - \frac{1}{2}mu^2 = F.S \quad \text{---(2)}$$

We can generalise equation (1) to three dimensions by employing vectors.

$$v^2 - u^2 = 2\vec{a} \cdot \vec{d}$$

Once again multiplying both sides by $\frac{m}{2}$ we get

$$\frac{1}{2}mv^2 - \frac{1}{2}mu^2 = m \vec{a} \cdot \vec{d} = \vec{F} \cdot \vec{d} \quad \text{-----}(3)$$

The above eq'n provides amotivation for the definition of work and K.E.

$$\text{in eq'n (3)} \quad \frac{1}{2}mv^2 - \frac{1}{2}mu^2 = K_f - K_i$$

where K_f, K_i are initial and final K.E. and $\vec{F} \cdot \vec{d} = W$

Where wrefers to work done by a force on the body over a certain displacement.

$$\therefore K_f - K_i = W \quad \text{-----}(4)$$

\therefore This is work - energy therorem.

2. What are collisions? Explain the possible types of collisions? Develop the theory of one-dimensional elastic motion?

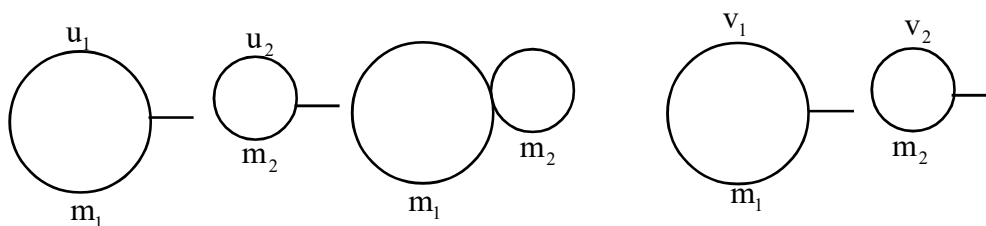
Ans:- **Collision** : A collision is a strong interaction between the particles with (or) with out contact when there are no other external forces.

Collision two types : 1) elastic collision (2) In elastic collisions.

(1) Elastic collision : The collision in which both momentum and kinctic energy are conserved then is called elastic collisions.

(2) In elastic collisions : The collision in which kinetic energy is not conservet but momentum is conserved, is called inelastic collision.

One-dimentional elastic collision : Consider two bodies of masses m_1 and m_2 moving with velocities u_1 and u_2 collide elastically. Assume $m_1 > m_2$ and $u_1 > u_2$. Let v_1 and v_2 be the velocities of the two bodies after collision.



From the law of consorvation of momentum.

$$m_1u_1 + m_2u_2 = m_1v_1 + m_2v_2$$

$$m_1(u_1 - v_1) = m_2(u_2 - v_2) \quad \text{-----}(1)$$

From the law of conservation of K.E.

$$\frac{1}{2}m_1u_1^2 + \frac{1}{2}m_2u_2^2 = \frac{1}{2}m_1v_1^2 + \frac{1}{2}m_2v_2^2$$

$$m_1(u_1^2 - v_1^2) = m_2(v_2^2 - u_2^2) \quad \text{-----}(2)$$

Dividing equation (2) and (1) then we get

$$\frac{(u_1 - v_1)(u_1 + v_1)}{(u_1 - v_1)} = \frac{(v_2 - u_2)(v_2 + u_2)}{(v_2 - u_2)}$$

$$u_1 + v_1 = v_2 + u_2$$

$$u_1 - u_2 = v_2 - v_1 \quad \text{----- (3)}$$

Velocity of first body

From eq'n (3) $v_2 = u_2 + v_1 - u_1$

Substituting eq'n (4) in eq'n (1) and simplifying, we get

$$v_1 = \left(\frac{m_1 - m_2}{m_1 + m_2} \right) u_1 + \left(\frac{2m_2}{m_1 + m_2} \right) u_2 \quad \text{----- (5)}$$

Velocity of second body

Again from equation (3) $v_1 = v_2 + u_2 - u_1$

Substituting this in eq'n (1) and simplifying, we get

$$v_2 = \left(\frac{2m_1}{m_1 + m_2} \right) u_1 + \left(\frac{m_2 - m_1}{m_1 + m_2} \right) u_2 \quad \text{----- (6)}$$

3. State and prove law of conservation of energy in case of a freely falling body?

Ans:- **Law of conservation of energy :**

Energy can neither be created nor be destroyed. But it can be changed from one form to another form.

Proof : Consider a body of mass "m" dropped from a height "n" above the ground.

At the point "A"

initial velocity = 0

$$\therefore \text{Kinetic energy } K.E_A = \frac{1}{2} m u^2 = 0$$

$$P.E_A = mgh$$

$$(h = H) \Rightarrow P.E_A = mgH$$

$$\therefore \text{Total Energy} = P.E_A + K.E_A \\ = mgH + 0$$

$$\boxed{T.E_A = mgH} \quad \text{----- (1)}$$

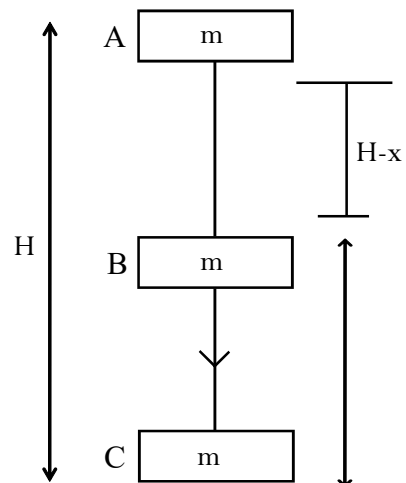
At the point "B" : Kinetic relation (3) eq'n

$$v^2 - u^2 = 2as \quad \mu = a$$

$$v_B^2 - 0^2 = 2(+g)(H - x) \quad v = v_B$$

$$v_B^2 = 2g(H - x) \quad a = +g$$

$$S = H - x$$



$$K.E_B = \frac{1}{2}mv_B^2 = \boxed{\frac{1}{2}m(u^2 - 2gh)}$$

$$= \frac{1}{2}m(2g(H-x)) \quad \boxed{\frac{1}{2}mu^2 - mgh}$$

$$K.E_B = mgH - mgx$$

$$P.E_B = mgh$$

$$h = x$$

$$P.E_B = mgx$$

$$T.E_B = mgH - mgx + mgx = mgH$$

$$\boxed{T.E_B = mgH} \quad \text{-----(2)}$$

At the point "C" : Kinematic relation to

$$v^2 - u^2 = 2as \quad v = v_c$$

$$v_c^2 = 2gH \quad u = 0$$

$$K.E_c = \frac{1}{2}mv_c^2 \quad a = g$$

$$= \frac{1}{2}m(2gH) \quad S = H$$

$$K.E_c = mgH$$

$$P.E_c = mgh$$

$$h = 0$$

$$P.E_c = 0$$

$$T.E_c = mgH + 0 = mgH$$

$$\boxed{T.E_c = mgH} \quad \text{-----(3)}$$

∴ in (1), (2) and (3) total mechanical energy remains constant. Hence law of conservation of energy is verified in the case of a freely falling body.

Problems :

1. A machine gun fires 360 bullets per minutes each bullet travels with a velocity of 600 m/s. If the mass of each bullet is 5 gr, find the power of the machine gun?

Ans:- $n=360$, $t=600\text{m/sec}$ $m=5\text{gr} = 5 \times 10^{-3}\text{kg}$

$$P = \frac{\frac{1}{2}mnv^2}{t} = \frac{\frac{1}{2} \times 5 \times 10^{-3} \times 360 \times 600 \times 600}{60}$$

$$P = 5400\text{W} \quad = 5.4\text{K.W}$$

2. Find the useful power used in pumping 3425m^3 of water per hour from a well 8m deep to the surface. Supposing 40% of the horse power during pumping is wasted. What is the horse power of the engine?

Ans:- $V = 3425\text{ m}^3 = d = 103\text{ Kg/m}^3$ $h=8\text{m}$ $g=9.8\text{m/s}^2$

$t = 1\text{ hour} = 60 \times 60\text{ sec.}$

$$\text{Power} = \frac{mgh}{t} \Rightarrow 60\% \text{ power} = \frac{mgh}{t}$$

$$\Rightarrow 60\% \text{ power} = \frac{vdgh}{t}$$

$$\Rightarrow \frac{60}{100} \times P = \frac{3425 \times 10^3 \times 9.8 \times 8}{60 \times 60}$$

$$P = \frac{3425 \times 10^3 \times 10^2 \times 9.8 \times 8}{60 \times 60 \times 60}$$

$$P = 1243.14\text{ watt}$$

$$\boxed{P = 1.666\text{ h.P}} \quad [\text{Thp} = 746\text{ watt}]$$

3. A pump is required to lift 600kg of water per minute from a well 25m deep and to eject it with a speed of 50 m/sec. Calculate the power required to perform the above task?

Ans:- $m = 60\text{ kg}$ $h=25\text{m,}$ $v = 50\text{m/sec}$ $t=60\text{sec}$

$$p = \frac{mgh + \frac{1}{2}mv^2}{t} = \frac{m \left[gh + \frac{1}{2}v^2 \right]}{t}$$

$$= \frac{600}{60} \left[9.8 \times 25 + \frac{50 \times 50}{2} \right] = 10 [245 + 1250]$$

$$= 14950\text{ watt}$$

$$\boxed{P = 14.95\text{ kw}}$$

4. From a height of 20m above a horizontal floor, a ball is thrown down with initial velocity 20 m/sec. After striking the floor, the ball bounces to the same height from which it was thrown. Find the coefficient of restitution for the collision between the ball and the floor?

Ans:- $u = 20\text{ m/sec,}$ $h = 20\text{m,}$ $g=10\text{m/s}^2$

$$v^2 - u^2 = 2as$$

$$u_1^2 - 20^2 = 2 \times 10 \times 10$$

$$u_1^2 = 20^2 + 400$$

$$u_1^2 = 400 + 400$$

$$\therefore u_1 = \sqrt{800}$$

5. A ball fall from a height of 10m on to a hard horizontal floor and repeatedly bounces. If the coefficient of restitution is $\frac{1}{\sqrt{2}}$, what is the total distance travelled by the ball before it ceases to rebounds?

Ans:- $e = \frac{1}{\sqrt{2}}, h = 10\text{m}$

$$S = h \left[\frac{1 + e^2}{1 - e^2} \right]$$

$$= 10 \left[\frac{1 + \frac{1}{2}}{1 - \frac{1}{2}} \right]$$

$$= 10 \times \frac{3}{2} \times \frac{2}{1}$$

$$\boxed{S = 30 \text{ m}}$$



UNIT VII

SYSTEMS OF PARTICLES AND ROTATIONAL MOTION

VERY SHORT QUESTION & ANSWERS (2 MARKS)

1. Is it necessary that a mass should be present at the center of mass of any system?

Ans:- No, any mass need not be present at the center of mass of a system.

Ex : a hollow sphere, center of mass lies at its center.

2. What is the difference in the positions of girl, carrying a bag in one of her hands and another girl carrying a bag in each of her two hands?

Ans:- For a girl with one bag in her hand the center of mass shifts (girl-bag system) towards the hand with the bag. For a girl with two bags in either of hands the position of center of mass system does not change.

3. Two rigid bodies have same moment of inertia about their axes of symmetry or the two, which body will have greater kinetic energy?

Ans:- $E = \frac{1}{2} I \omega^2 = \frac{1}{2} \frac{L^2}{I}$, $E \propto \frac{1}{I}$ ($\because L = \text{constant}$)

The rigid body having less moment of inertia will have greater K.E.

4. Why are spokes provided in a bicycle wheel?

Ans:- By connecting to the rim of wheel to the axle through the spokes the mass of the wheel gets concentrated at its rim. This increases its moment of inertia. This ensures its uniform speed.

5. We cannot open or close the door by applying force at the hinges. Why?

Ans:- When the force is applied at the hinges, the line of the force passes through the axis of rotation. i.e. $r = 0$, So we can not open or close the door by pushing or pulling it at the hinges.

6. Why do we prefer a spanner of longer arm as compared to the spanner of shorter arm?

Ans:- The torque applied on the nut by the spanner is equal to the force multiplied by the perpendicular distance from the axis of rotation. A spanner with longer arm provides more torque compared to a spanner with shorter arm. Hence longer arm spanner is preferred.

7. By spinning egg on a table top, how will you distinguish a hard boiled egg from a raw egg?

Ans:- A raw egg has some fluid in it and a hard boiled egg is solid form inside. Both eggs are spinning on a table top. The fluid is thrown outwards. Therefore $I_r > I_b$. That means M. I of raw egg is greater than boiled egg. As $I \times \omega$ constant.

$\therefore \omega_r < \omega_b$ That means angular velocity of raw egg is less than angular velocity of boiled egg.

8. Why should a helicopter necessarily have two propellers?

Ans:- If there were only one propeller in the helicopter then, due to conservation of angular momentum, the helicopter itself would have turned in the opposite direction.

9. If the polar ice caps of the earth were to melt, what would the effect of the length of the day be?

Ans:- Earth rotates about its polar axis when ice of polar caps of earth melts, mass concentrated near the axis or rotation spreads out. Therefore, moment of inertia, I increases. As no external torque acts

$\therefore L = I \times \omega = I \left(\frac{2\pi}{T} \right) = \text{constant}$ with increases of I , T will increase i.e. length of the day will increase.

10. Why is it easier to balance a bicycle in motion?

Ans:- When bicycle is in motion, it is easy to balance because the principle of conservation of angular momentum is involved.

SHORT QUESTION & ANSWERS (4MARKS)

1. Distinguish between center of mass and center of gravity?

Center of mass	Center of gravity
1. Point at which entire mass of the body is supposed to be concentrated and the motion of the point represents motion of the body	1. Fixed point through which the weight of the body acts.
2. It refers mass of the body.	2. It refers to the weight acting on all particles of the body.
3. In a uniform gravitational field center of mass and gravity coincide.	3. In a non-uniform gravitational field, center of gravity and CM do not coincide.
4. CM of the body is defined to describe the nature of motion of a body as a whole.	4. Center of gravity of body is defined to know the amount of stability of stability of the body when supported.

2. Show that a system of particle moving under the influence of an external force, moves as if the force is applied at its center of mass?

Ans:- Let us consider position vector's $\vec{x}_1, \vec{x}_2, \dots, \vec{x}_n$ are and masses m_1, m_2, \dots, m_n particles system.

According to definition of center of mass

$$\vec{X} = \frac{m_1 \vec{x}_1 + m_2 \vec{x}_2 + \dots + m_n \vec{x}_n}{m_1 + m_2 + \dots + m_n}$$

$$\text{Consider } m_1 + m_2 + \dots + m_n = M$$

$$\vec{X} = \frac{m_1 \vec{x}_1 + m_2 \vec{x}_2 + \dots + m_n \vec{x}_n}{M}$$

$$M\vec{X} = m_1 \vec{x}_1 + m_2 \vec{x}_2 + \dots + m_n \vec{x}_n$$

Differentiating on both sides above eq'n.

$$M \frac{d\vec{X}}{dt} = m_1 \frac{d\vec{x}_1}{dt} + m_2 \frac{d\vec{x}_2}{dt} + \dots + m_n \frac{d\vec{x}_n}{dt}$$

$$M \vec{v} = m_1 \vec{v}_1 + m_2 \vec{v}_2 + \dots + m_n \vec{v}_n$$

Differentiating on both sides above eq'n.

$$M \frac{d\vec{v}}{dt} = m_1 \frac{d\vec{v}_1}{dt} + m_2 \frac{d\vec{v}_2}{dt} + \dots + m_n \frac{d\vec{v}_n}{dt}$$

$$\text{But } m_1 \vec{a}_1 = \vec{F}_1, m_2 \vec{a}_2 = \vec{F}_2, \dots, m_n \vec{a}_n = \vec{F}_n \text{ and}$$

$$M \vec{a} = \vec{F} \text{ then}$$

$$\vec{F} = \vec{F}_1 + \vec{F}_2 + \dots + \vec{F}_n$$

Where \vec{F}_{ext} represents the sum of all external forces acting on the particles of the system. This eq'n states that the C.M. of a system of particles moves as if all the mass of the system was concentrated at the center of mass and all external forces were applied at that point.

3. Explain about the center of mass of earth moon system and rotation around the sun.

Ans:- The earth moon system rotates about the common center of mass. The mass of the earth is about 81 times that of the moon. Hence the center of mass of the earth moon system is relatively close to the earth. The gravitational attraction of the sun is an external force that acts on the earth moon system. The center of mass of the earth-moon system moves in an elliptical path around the sun.

4. Define vector product. Explain the properties of a vector product with two Examples?

Ans:- **Vector product** : The cross product of two vectors is given by $\vec{C} = \vec{A} \times \vec{B}$ the magnitude of vector defined from cross product of two vectors is equal to product of magnitudes of the vectors and sine of angle between the vectors.

$$\vec{a} \times \vec{b} = ab \sin \theta \cdot \hat{n} \text{ where } \hat{n} \text{ is a unit vector along } \vec{a} \times \vec{b}$$

Properties :

i) Cross product of vectors do not obey commutative law.

$$\vec{A} \times \vec{B} \neq \vec{B} \times \vec{A} \text{ and } \vec{A} \times \vec{B} = -\vec{B} \times \vec{A}$$

ii) Cross product obey distributive law.

$$\vec{A} \times (\vec{B} \times \vec{C}) = \vec{A} \times \vec{B} \times \vec{C} = -\vec{B} \times \vec{A}$$

iii) The cross product of two parallel vectors is a null vector. If $\theta = 0^\circ$, then $\vec{A} \times \vec{B} = 0$

iv) The area of the triangle formed by \vec{A} and \vec{B} as adjacent sides is $\frac{1}{2} |\vec{A} \times \vec{B}|$

Examples :

1) Torque is cross product of position vector and force i.e. $\vec{\tau} = \vec{r} \times \vec{F}$

2) Angular momentum is cross product of position vector and momentum.

$$\vec{L} = \vec{r} \times \vec{P}$$

5. Define angular velocity (u) Derive $\omega = v/r$.

Ans:- **Angular velocity** : The rate of change of angular displacement of a body is called angular

velocity $\boxed{\omega = \frac{d\theta}{dt}}$

Equation : Consider a rigid body be moving with uniform speed (v) along the circumference of a circle of radius r. Let the body be displaced from A to B in a small interval of time Δt making an angle $\Delta\theta$ at the center. Let the linear displacement be Δx from A to B.

From the property length of arc = radius \times angle.

$$\Delta x = r \Delta\theta$$

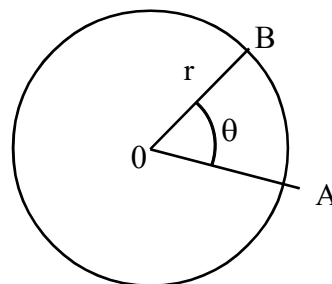
This equation is divided by Δt , and taking

Limit $\Delta t \rightarrow 0$ on both sides.

$$\Rightarrow \lim_{\Delta t \rightarrow 0} \frac{\Delta x}{\Delta t} = r \lim_{\Delta t \rightarrow 0} \frac{\Delta\theta}{\Delta t} \text{ ----- (1)}$$

$$\text{But } \lim_{\Delta t \rightarrow 0} \frac{\Delta x}{\Delta t} = v \text{ ----- (2) and } \lim_{\Delta t \rightarrow 0} \frac{\Delta\theta}{\Delta t} = \omega \text{ ----- (3)}$$

eq'n (2) & (3) in (1) we get $\boxed{r = v \cdot \omega}$



6. **Define angular acceleration and torque. Establish the relation between angular acceleration and torque?**

Ans:- **Angular acceleration :** The rate of change of angular velocity is called angular acceleration

$$\text{i.e. } \alpha = \frac{d\omega}{dt}$$

Torque : The rate of change of angular momentum is called torque or the moment of force is called torque.

Relation between angular acceleration and Torque :

Consider a rigid of mass "M"

rotating in a circular path of radius "R"

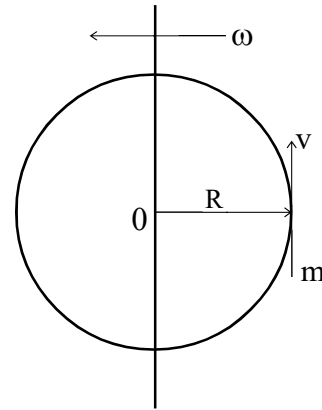
with angular velocity about fixed axis.

$$\text{By definition, } \tau = \frac{dL}{dt} = \frac{d}{dt} (I\omega)$$

Where $I = MR^2$ = Momentum of inertia of a body.

$$\tau = I \frac{d\omega}{dt} \quad \left(\because \frac{d\omega}{dt} = \alpha \right)$$

$$\boxed{\tau = I \alpha}$$



7. **Write the equations of motion for a particular rotating about a fixed axis?**

Ans:- Equations of motion for a particle rotating about a fixed axis:

$$1) \quad \omega_f = \omega_i + \alpha t \quad \left[\because \text{like } v = u + at \right]$$

$$2) \quad \theta = \left(\frac{\omega_i + \omega_f}{2} \right) t \quad \left[\because \text{like } \vec{v} = \left(\frac{v_1 + v_2}{2} \right) t \right]$$

$$3) \quad \theta = \omega_i t + \frac{1}{2} \alpha t^2 \quad \left[\because \text{like } S = ut + \frac{1}{2} at^2 \right]$$

$$4) \quad \omega_f^2 - \omega_i^2 = 2 \alpha \theta \quad \left[\because \text{like } \omega^2 - u^2 = 2as \right]$$

8. **Derive expressions for the final velocity and total energy of a body rolling with out slopping?**

Ans:- **Expression of velocity of a body Rolling down an inclined place :** Consider a rigid body of mass M and radius R rolling down an inclined plane from a height h. Let v the linear speed acquired by the body when it reaches the bottom of the plane and K is its radius of gyration.

According to law of conservation of energy we have P.E of body on top of inclined plane.

$$\text{P.E. at the top} = \text{K.E. of translation} + \text{K.E. of rotation} \quad Mgh = \frac{1}{2}mv^2 + \frac{1}{2}I\omega^2$$

$$Mgh = \frac{1}{2}mv^2 + \frac{1}{2}mk^2 \frac{V^2}{R^2} \left(\begin{array}{l} I = MK^2 \\ \& \omega = \frac{V}{R} \end{array} \right)$$

$$Mgh = \frac{1}{2}M V^2 \left(1 + \frac{K^2}{R^2} \right)$$

$$\therefore V = \sqrt{\frac{2gh}{\left(1 + \frac{K^2}{R^2}\right)}}$$

Expression of total energy of a body rolling down on an inclined plane : Suppose a body is rolling on a surface. Its motion can be treated as a combination of the translation of the center of mass and rotation about an axis passing through the center of mass. The total K.E. can be written as.

$$E = E_T + E_R = \frac{1}{2}M V^2 + \frac{1}{2}I\omega^2 = \frac{1}{2}M R^2 \omega^2 + \frac{1}{2}M K^2 \omega^2$$

$$E = \frac{1}{2}M \omega^2 (R^2 + K^2)$$

$$E = \frac{1}{2}M \omega^2 \left(1 + \frac{K^2}{R^2} \right) \quad \text{gyration} \quad \left[\because \omega = \frac{V}{R} \right]$$

LONG QUESTION & ANSWERS (8MARKS)

1. (a) State and prove parallel axes theorem.
- (b) For a thin flat circular disk, the radius of gyration about a diameter as axis is K . If the disk is cut along a diameter AB as shown into two equal pieces, then find the radius of gyration of each piece about AB .

Ans:- **Statement :** The moment of inertia of a plane lamina about an axis is equal to the sum of the moment of inertia about a parallel axis passing through the center of mass and product of its mass and square of the distance between the two axes

$$\text{i.e. } I_0 = I_G + MR^2$$

Let I_G is the moment of inertia of the plane lamina about the axis Z_2 passing through the centre of mass.

I_0 is the moment of inertia of the lamina about an axis Z_1 .

Proof : Let a particle of mass m is situated at P . Moment of inertia about the axis passing through P with line extending from OG .

From the triangle ΔPOQ

$$OP^2 = OQ^2 + PQ^2$$

$$OP^2 = (OG + GQ)^2 + PQ^2$$

$$[\because OQ = OG + GQ]$$

$$OP^2 = OG^2 + 2OG \cdot GQ + GQ^2 + PQ^2$$

$$OP^2 - OG^2 + GP^2 + 2OG \cdot GQ$$

Multiplying with $\sum m$ on both sides.

$$\sum m OP^2 = \sum m OG^2 + \sum M GP^2 + \sum m OG \cdot GQ$$

$$\text{But } \sum m OG^2 = M r^2$$

(\because OG is constant and $\sum = M$ total mass of the body)

$$\sum m GP^2 = I_G, \quad \sum m OP^2 = I_0$$

$$I_0 = M r^2 + I_G + 2r \sum m GQ$$

$$\sum m \cdot GQ = 0$$

(\because The moment of all the particles about the center of mass is always zero)

$$\boxed{I_0 = I_G + M r^2}$$

(b) For the circular disk, the radius of gyration about a diameter AB is $K = \sqrt{\frac{I}{M}}$

The disk is cut into two halves about AB .

When each Mass $M = \frac{M}{2}$ and each M.I. $I = \frac{I}{2}$

Therefore radius of gyration of each piece is

$$K' = \sqrt{\frac{I'}{M'}} = \sqrt{\frac{\frac{I}{2}}{\frac{M}{2}}} = \sqrt{\frac{I}{M}} = K$$

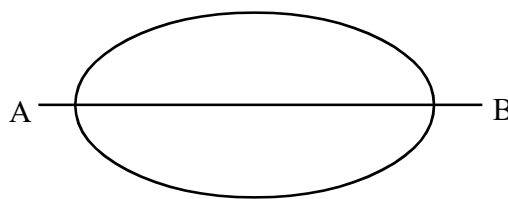
2. State and prove perpendicular axes theorem.

Ans:- **Statement :** The sum of moment of inertia of a plane lamina about any two perpendicular axes in its plane is equal to its moment of inertia passing through the point of intersection of the first two axes.

Proof : Consider a plane lamina revolving about the z-axis. Let "O" be the origin of the axis. Imagine a particle of mass "m" lying at a distance "r" from point "O" on the plane.

Let : x, y be the coordinates of the point P.

$$\text{Thus } r^2 = x^2 + y^2$$



Then the moment of the body about x-axis

$$I_x = \sum my^2$$

The moment of inertia of the body about

y - axis

$$I_y = \sum mx^2$$

Then the moment of inertia of the body about Z - axis

$$I_z = \sum mr^2 = \sum m(x^2 + y^2)$$

$$I_z = \sum mx^2 + \sum my^2$$

$$\therefore I_z = I_y + I_x$$

$$I_z = I_x + I_y$$

Hence perpendicular axes theorem is proved.

(b) If a thin circular ring and a thin flat circular disk of same mass have same moment of inertia about their respective diameters as axes. Then find the ratio of their radii.

For a thin circular M.I $I_r = \frac{MR^2}{2}$

For a thin flat circular disk M.I, $I_d = \frac{MR_d^2}{4}$

$$I_r = I_d$$

$$\Rightarrow \frac{MR_r^2}{2} = \frac{MR_d^2}{4} \Rightarrow \frac{R_r^2}{R_d^2} = \frac{2}{4} = \frac{1}{2}$$

$$\frac{R_r}{R_d} = \frac{1}{\sqrt{2}}$$

3. State and prove the principle of conservation of angular momentum. Explain the principle of conservation of angular momentum with example?

Ans:- **Statement :** Angular momentum of a body remains constant when the external torque is zero.

$$L = I\omega = \text{constant } K \text{ (or) } I_1\omega_1 = I_2\omega_2$$

If the moment of inertia of a body is lowered, the angular velocity of the body ω increases.

Proof : By definition, the rate of change of angular momentum is called Torque.

$$\tau = \frac{dL}{dt}$$

$$\text{If } \tau = 0 \Rightarrow \frac{dL}{dt} = 0 \quad (\because L = \text{constant})$$

$$L_1 = L_2$$

$$I_1\omega_1 = I_2\omega_2$$

Examples : 1) A ballet dancer decreases or increases his angular speed of rotation by stretching the hands or bringing the hands close to the body.

2) A diver jumps from a diving board with both the legs and hands kept far off from the body.

The diver then brings the hands and legs close to the body increasing the angular velocity.

The diver makes rotation in air. When the diver nears the water, legs and hand are stretched so that moment of inertia increases and ω decreases.

Problems :

- Three particles each of mass 100g are placed at the vertices of an equilateral triangle of side length 10 cm. Find moment of inertia of the system about an axis passing through the centroid of the triangle and perpendicular to its plane.

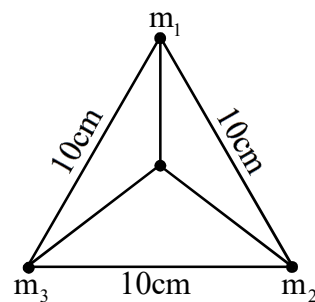
Ans:- $m = 100\text{g}, \quad = 100 \times 10^{-3}\text{kg}$ side $a = 10\text{cm}$

Moment of inertia $= I = 3mr^2$

$$I = 3 \times 100 \times 10^{-3} \times \left[\frac{10}{\sqrt{3}} \times 10^{-2} \right]^2$$

$$= \frac{3 \times 10^{-1} \times 10^2 \times 10^{-4}}{3}$$

$$I = 10^{-3} \text{ kgm}^2$$



- Two uniform circular disks each of mass 1 kg and radius 20 cm, are kept in contact about the tangent passing through the point of contact. Find the moment of inertia of the tangent passing through the point of contact.

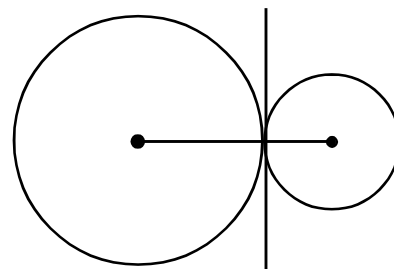
Ans:- Mass $= m = 1\text{kg}$ $r = 20\text{ cm}$

$$I = I_1 + I_2 = 20 \times 10^{-2} \text{ cm}$$

$$I_1 = \frac{MR^2}{4} + MR^2 = \frac{5MR^2}{4}$$

$$I_2 = \frac{5MR^2}{4}$$

$$I = \frac{10MR^2}{4} = \frac{10 \times 1 \times (20 \times 10^{-2})^2}{4} = 0.1 \text{ Kg m}^2$$



- Four spheres each of diameter $2a$ and mass " m " are placed with their centers at the four corners of a square of side b . Calculate the moment of inertia of the system about any side of the square?

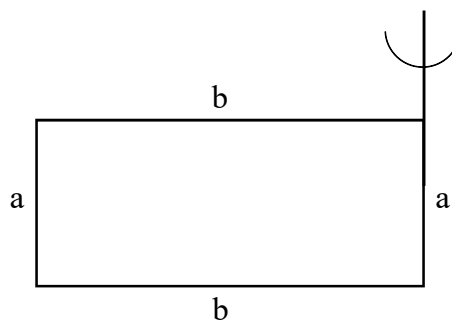
Ans:- $I_1 = mb^2$, $I_2 = \frac{2}{5}mb^2$, $I_3 = \frac{2}{5}mb^2$, $I_4 = mb^2$

Momantum of inertia of the

System $I = I_1 + I_2 + I_3 + I_4$

$$= mb^2 + \frac{2}{5}mb^2 + \frac{2}{5}mb^2 + mb^2$$

$$I = \frac{4}{5}mb^2 + 2mb^2$$



4. Determine the K.E of a circular disc rotating with a speed of 60 rpm about an axis passing through a point on its circumference and perpendicular to its plane. The circular disc has a mass of 5kg and radius 1m.

Ans:- Hence $M = 5\text{kg}$, $R = 1\text{m}$, $\omega = 2\pi \times \frac{N}{t} = 2\pi \times \frac{60}{60} \text{ rad/sec}$

$$= 2\pi \text{ rad/sec.}$$

The M.I of disc about paralld axis

Pasing through apoint on its circumberance.

$$I = \frac{MR^2}{2} + MR^2 = \frac{3MR^2}{2}$$

$$\text{K.E} = \frac{1}{2}I\omega^2 = \frac{1}{2} \times \frac{3}{2} M^2\omega^2 = \frac{3}{4} \times 5 \times 1^2 \times (2\pi)^2$$

$$= \frac{3}{4} \times 5 \times 4 \times (3.14)^2$$

$$\text{K.E} = 148.16 \text{ J}$$

5. The momentumot incrtia of a fly wheel making 300 revolutions per minute is 0.3 kg m^2 . Find the torque required to bring it to rest in 20sec.

Ans:- Here $I = 0.3\text{kgm}^2$ $\frac{N}{t} = \frac{300 \text{ revontions}}{1 \text{ min tues}}$

$$\omega_i = \frac{2\pi N}{t} = \frac{2\pi \times 300}{60} = 10\pi \text{ rad/sec}$$

$$t = 20 \text{ sec}, \quad \omega_f = 0, \quad \tau = ?$$

$$\tau = I \alpha = I \left(\frac{\omega_f - \omega_i}{t} \right) = 0.3 \left(\frac{0 - 10\pi}{20} \right)$$

$$= \frac{-0.3\pi}{2}$$

$$= -0.471 \text{ N.m}$$

6. Find the center of mass three particules at the vretices of an equilateral tri-
angle. The masses of the particles are 100, 150 and 200 gr respectively. Each side
of the equilateral triangle is 0.5 long.

Ans:- The coordinate points are O,A,B

and respectively (0,0) (0,5,0)

(0.25, 0.25√3), it following masses are 100, 150, 200g

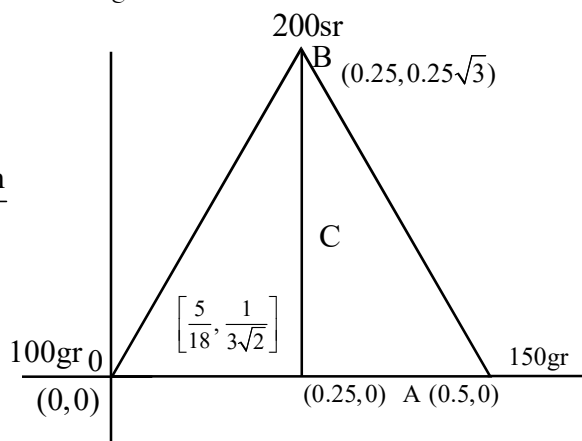
$$X = \frac{m_1 x_1 + m_2 x_2 + m_3 x_3}{m_1 + m_2 + m_3}$$

$$= \frac{(100(0) + 150(0.5) + 200(0.25)) \text{ gm}}{[100 + 150 + 200] \text{ g}}$$

$$= \frac{75 + 50}{450} \text{ m} = \frac{125}{450} \text{ m} = \frac{5}{18} \text{ m}$$

$$Y = \frac{(100(0) + 150(0) + 200(0.25\sqrt{3})) \text{ gm}}{450 \text{ g}}$$

$$= \frac{50\sqrt{3}}{450} \text{ m} = \frac{\sqrt{3}}{9} \text{ m} = \frac{1}{3\sqrt{3}} \text{ m}$$



7. Find the scalar and vector product of two vector?

$$\mathbf{a} = 3\vec{i} - 4\vec{j} + 5\vec{k} \text{ and } \mathbf{b} = 2\vec{i} + \vec{j} - 3\vec{k}$$

Ans:- $\mathbf{a} \cdot \mathbf{b} = (3\vec{i} - 4\vec{j} + 5\vec{k}) \cdot (2\vec{i} + \vec{j} - 3\vec{k}) = -6 - 4 - 15$

$$= -25$$

$$\mathbf{a} \times \mathbf{b} = \begin{vmatrix} \vec{i} & \vec{j} & \vec{k} \\ 3 & -4 & 5 \\ -2 & 1 & -3 \end{vmatrix} = 7\vec{i} - \vec{j} - 5\vec{k}$$

8. Find the torque of a force about the origin. The force acts on a particle whose
position vector is $\vec{i} - \vec{j} + \vec{k}$.

Ans:- Here $\mathbf{r} = \vec{i} - \vec{j} + \vec{k}$, $\mathbf{F} = 7\vec{i} - 3\vec{j} + 5\vec{k}$

$$\boldsymbol{\tau} = \mathbf{r} \times \mathbf{F} = \begin{vmatrix} \vec{i} & \vec{j} & \vec{k} \\ 1 & -1 & 1 \\ 7 & 3 & -5 \end{vmatrix} = (5 - 3)\vec{i} - (-5 - 7)\vec{j} + (3 - (-7))\vec{k}$$

$$\boldsymbol{\tau} = 2\vec{i} + 12\vec{j} + 10\vec{k}$$



UNIT VIII

OSCILLATIONS

VERY SHORT QUESTION & ANSWERS (2 MARKS)

1. Give two examples of periodic motion are not oscillatory?

Ans:- (i) The motion of planet around the sun (ii) Revolution of electrons around the nucleus.

2. The displacement in S.H.M is given by $y = a \sin (20t + 4)$ what is the displacement when it is increased by $\frac{2\pi}{w}$?

Ans:- $y = a \sin (20t + 4)$

$T = \frac{2\pi}{w}$ is increased, the displacement of the particle remains the same.

3. A girl is swinging seated in a swing. What is the effect on the frequency of oscillation if she stands?

Ans:- Frequency $n = \frac{1}{2\pi} \sqrt{\frac{g}{l}} \propto \frac{1}{\sqrt{l}}$

A girl swinging in standing position location of center of masses shifts upwards l decreases, frequency of oscillation increases.

4. The bob of a simple pendulum is a hollow sphere filled with water, how will the period of oscillation change, if the water begins to drain out of the hollow sphere?

Ans:- The time period will increase at first, then decreases until the sphere is empty, finally the period will be the same as when the sphere was full of water.

5. The bob of a simple pendulum is made of wood. What will be the effect on the time period if the wooden bob is replaced by an identical bob of aluminum?

Ans:- Time period $T = 2\pi \sqrt{\frac{L}{g}}$ Time period is independent of mass of the bob. Hence wooden bob is replaced by an identical aluminium bob, time period remains constant.

6. Will a pendulum clock gain or lose time when taken to the top of mountain?

Ans:- At higher altitudes i.e. on mountain the acceleration due to gravity is less compared to the ground. The time period increases. The pendulum clock loses time on mountain.

7. A pendulum clock gives correct time at the equator will it gain or lose time if it is taken to the poles? If so why?

Ans:- Time period $= T = 2\pi \sqrt{\frac{\ell}{g}}$, g value at poles greater than at equator, if it is taken to the poles g value increases time period decreases. So pendulum clock gain time.

8. What fraction of the total energy is K.E. when the displacement is one half of an amplitude of a particle executing SHM?

Ans:- Total energy K.E $= \frac{1}{2} m \omega^2 x^2$

$$y = \frac{A}{2} \Rightarrow \text{K.E} = \frac{1}{2} m \omega^2 (x^2 - y^2) = \frac{1}{2} m \omega^2 \left(A^2 - \frac{A^2}{4} \right)$$

$$\text{K.E} = \frac{3}{4} \times \frac{1}{2} m \omega^2 A^2$$

$$\text{K.E} = \frac{3}{4} \times E \Rightarrow \frac{\text{K.E.}}{E} = \frac{3}{4}$$

9. What happens to the energy of a simple harmonic oscillator if its amplitude is doubled.

Ans:- Total energy $E = \frac{1}{2} m \omega^2 A^2$

given amplitude A is doubled.

$$E' = \frac{1}{2} m \omega^2 (2A)^2 = \frac{1}{2} m \omega^2 4A^2$$

$$= 4 \times \frac{1}{2} m \omega^2 A^2$$

\therefore Energy becomes four times $E' = 4 \times E$

10. Can a simple pendulum be used in an artificial satellite?

Ans:- No, It does not oscillate. This is because there exists a state of weightlessness in a satellite.

SHORT QUESTION & ANSWERS (4MARKS)

1. Define simple harmonic motion. Give two examples?

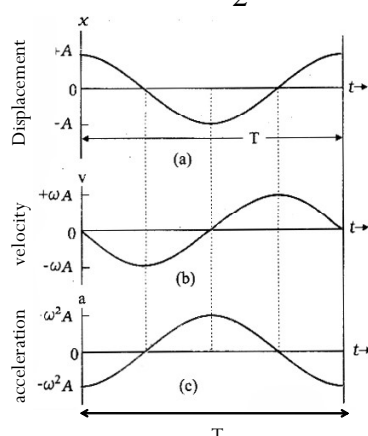
Ans:- **Simple Harmonic motion** : "A body is said to be in simple harmonic motion, if it moves to and fro along a straight line, about its mean position such that at any point its acceleration is proportional to its displacement but opposite in direction and is directed always towards the mean position".

$$a \propto -y$$

- Examples :
- 1) Motion of a simple pendulum.
 - 2) Motion of mass attached to a spring
 - 3) Motion of atoms in solids.
 - 4) Cork floating on water.

2. Present graphically the variation of displacement, velocity and acceleration with time for a particle in SHM?

Ans:- Displacement, velocity phase difference $\frac{\pi}{2}$ and acceleration, displacement phase difference is π .



3. What is phase? Discuss the phase relations between displacement, velocity and acceleration in simple harmonic motion?

Ans:- Phase : The phase of a particle executing S.H.M. at any instant is defined as its state (or) condition regards to its position and direction.

- i) Displacement : $x = A \cos (wt - \phi)$, $(wt - \phi)$ is called phase and is epoch.
- ii) Velocity : $V = -Aw \sin (wt - \phi)$, Here also $(wt - \phi)$ is phase angle.
- iii) accelerations : $a = -Aw^2 \cos (wt - \phi)$ Here also $(wt - \phi)$ is phase angle.

4. Obtain an equation for the frequency of oscillation of spring of force. Constant K to which a mass m is attached?

Ans:- Let us consider a spring suspended vertically from a rigid support and loaded with a mass if it is now pulled down and released, it executes vertically oscillations about mean position.

Restoring force is directly proportional to the displacement, but oppositely directed

$$F \propto -y \Rightarrow F = -K_y \text{ ----- (1)}$$

from Newton's 2nd laws to

$$F = ma \text{ ----- (2)}$$

$$(1) = (2)$$

$$Ma = -k$$

$$a = -\left(\frac{k}{M}\right)y \text{ ----- } \rightarrow (2)$$

We can write $a \propto -y$

i.e Acceleration is directly proportional to displacement but oppositely directed.

$$\Rightarrow a = -\omega^2 y \quad \text{----- (3)}$$

Comparing above eq'n (2) & (3)

$$\omega^2 = \frac{K}{M} \Rightarrow \omega = \sqrt{\frac{K}{M}}$$

$$\text{But } T = \frac{2\pi}{\omega} \Rightarrow T = 2\pi \sqrt{\frac{M}{K}}$$

$$\text{Frequency of oscillation } n = \frac{1}{2\pi} \sqrt{\frac{K}{M}}$$

5. Derive expressions for the kinetic energy and potential energy of a simple harmonic oscillator?

Ans:- K.E. of S.H Oscillator : The velocity of a particle in S.H.M is given by $V = \omega \sqrt{A^2 - y^2}$

$$\text{K.E} = \frac{1}{2} mv^2 = \frac{1}{2} m \omega^2 (A^2 - y^2)$$

$$\text{when } y = 0 \Rightarrow \text{K.E}_{\max} = \frac{1}{2} m \omega^2 A^2 \quad (\text{Mean position})$$

$$\text{when } y = A \Rightarrow \text{K.E}_{\min} = 0 \quad (\text{Extreme position})$$

P.E of simple harmonic oscillator : When the displacement of a particle executing S.H.M. increases the restoring force also increases. The restoring force is in the opposite direction to the displacement. Therefore work is done in moving through the displacement against restoring force. If F is the restoring force at the displacement y .

$$\text{The average force against which work is done} = \frac{0 + F}{2} = \frac{F}{2}$$

Work done on the particle for the displacement = average force \times displacement

$$W = \frac{F}{2} \times y$$

$$W = \frac{m a y}{2} \quad \text{----- (1)} \quad (\because F = m a)$$

But acceleration of a particle in S.H.M. is given by

$$a = -\omega^2 y \rightarrow (2)$$

using (1) & (2) eq'n we get

$$\text{The work done (W)} = \frac{1}{2} m \omega^2 y^2$$

The work done $\Rightarrow P.E = \frac{1}{2}mw^2y^2$ ----- (3)

if $y = 0$, $P.E_{\min} = 0$ (Mean position)

$y = A$, $P.E_{\max} = \frac{1}{2}mw^2A^2$ (extreme position)

6. How does the energy of a simple pendulum vary as it moves from one extreme position to the other during its oscillations?

Ans:- The total energy associated with a particle executing S.H.M at any point is the sum of potential energy and K.E. at that point.

Total energy = K.E + P.E

$P.E = \frac{1}{2}mw^2y^2$

$K.E = \frac{1}{2}mw^2(A^2 - y^2)$

$\therefore T.E = \frac{1}{2}mw^2(A^2 - y^2) + \frac{1}{2}mw^2y^2$

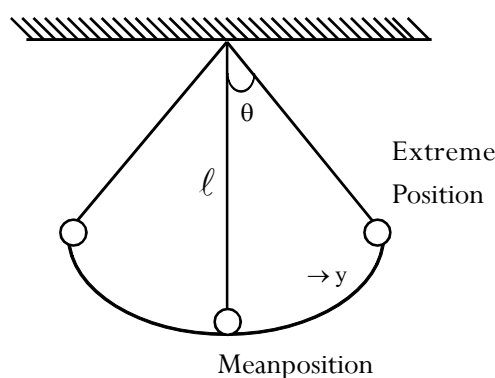
$T.E = \frac{1}{2}mw^2A^2$

At mean position $y = 0$, $P.E = 0$

and $K.E_{\max} = \frac{1}{2}mw^2A^2$, $T.E = 0 + \frac{1}{2}mw^2A^2 = \frac{1}{2}mwA^2$

At extreme position $y = A$, $K.E = 0$, $P.E_{\max} = \frac{1}{2}mw^2A^2$

From mean position to extreme position K.E. is to be converted into P.E.



7. Derive the expression for displacement velocity and acceleration of a particle executes S.H.M?

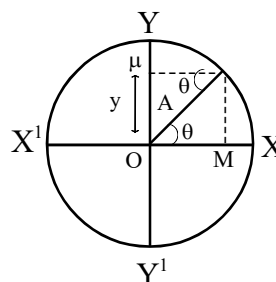
Ans:- Consider a particle moves on the circumference of a circle of radius A with uniform angular velocity w . Let PN be the perpendicular drawn to the diameter yy' to and from about the center O .

Let $\angle POX = \theta$, $OP = A$, $ON = y$

From ΔONP , $\sin wt = \frac{ON}{OP}$

$ON = OP \sin wt$

$y = A \sin wt \rightarrow (1)$



Velocity : The rate of change of displacement is known as velocity.

$$v = \frac{dy}{dt} = \frac{d}{dt} (A \sin \omega t) = A\omega \cos \omega t = A\omega \sqrt{1 - \sin^2 \omega t}$$

$$\therefore V = A\omega \sqrt{1 - \left(\frac{y}{A}\right)^2} \quad \left[\because \sin \omega t = \frac{y}{A} \right]$$

$$v = \omega \sqrt{A^2 - y^2} \rightarrow (2)$$

acceleration : The rate of change of velocity is known as acceleration.

$$a = \frac{dv}{dt} = \frac{d}{dt} (A\omega \cos \omega t)$$

$$= -A\omega^2 \sin \omega t \quad (\because y = A \sin \omega t)$$

$$a = -\omega^2 y \quad \text{---} \rightarrow (3)$$

LONG QUESTION & ANSWERS (8MARKS)

1. Define S.H.M show that the motion of (point) projection of a particle performing uniform circular motion, on any diameter, is simple harmonic?

Ans:- Simple Harmonic motion : A body is said to be in simple harmonic motion, if it moves to and fro along a straight line, about its mean position such that, at any point its acceleration is proportional to its displacement but opposite in direction and directed always towards the mean position.

$$a \propto -y$$

Show that the projection of uniform circular motion on any diameter is simple harmonic :

- consider a particle p moving on the circumference of a circle of radius A with uniform angular velocity ω . Let O be the center of the circle xx' and yy' are two mutually perpendicular diameters of the circle as shown in figure let PN be drawn perpendicular to the diameter yy' from P. As P moves on the circumference of the circle. N moves on the diameter yy' to and fro about the center O. Let us consider the position of N at any time t, after leaving the point "O" during its motion. The corresponding angular displacement of the particle p is $\angle xOP = \theta = \omega t$

$$\text{From } \triangle ONP \Rightarrow \sin \omega t = \frac{ON}{OP}$$

$$ON = OP \sin \omega t \quad (ON = y \quad OP = A)$$

$$y = A \sin \omega t \quad \text{---} \rightarrow (1)$$

Differentiating eq'n (1) w.r.t "t" we get

$$\text{Velocity } v = \frac{dy}{dt} = \frac{d}{dt} (A \sin \omega t)$$

$$v = A\omega \cos \omega t = A\omega \sqrt{1 - \sin^2 \omega t} \text{ ----- (2)}$$

$$= A\omega \sqrt{1 - \frac{y^2}{A^2}} \quad \left(\because \sin \omega t = \frac{y}{A} \right)$$

$$v = \omega \sqrt{A^2 - y^2} \text{ ----- (3)}$$

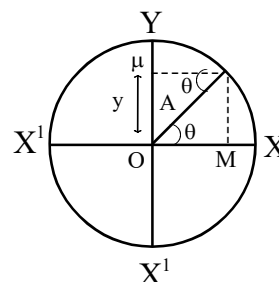
Again Differentiating eq'n (2) w.r. + 't' we get acceleration

$$a = \frac{dv}{dt} = \frac{d}{dt} (A\omega \cos \omega t)$$

$$= -A\omega^2 \sin \omega t \quad (\because y = A \sin \omega t)$$

$$a = -\omega^2 y \text{ ----- (4)}$$

$$a \propto -y \text{ ----- (5)}$$



2. Show that the motion of a simple pendulum is simple harmonic and hence derive an equation for its time period. what is seconds pendulum?

Ans:- **Simple pendulum** : A heavy metal point mass suspended by a light inextensible string is called an ideal simple pendulum.

Consider a simple pendulum with a metal bob of mass "m". Let "s" be the point of suspension and "l" be the length of the pendulum. Let the bob be given a small angular displacement " θ " and released. Let "A" be the mean position and "B" be the extreme position. Let $AB = x =$ Displacement from the mean position.

$$AB = x = l\theta \text{ (or) } \theta = \left(\frac{x}{l} \right) \text{ ----- (1)}$$

At point "B" the force acting on the bob are

i) The weight of the bob ' mg ' vertically down wards, this can be resolved into two rectangular components $mg \cos \theta$ and $mg \sin \theta$ as shown in figure.

ii) The tension in the string 'T' the tension T in the string balances the components $mg \cos \theta$.

Restoring force on the bob $F = -mg \sin \theta$

$$\text{Acceleration } a = \frac{-mg \sin \theta}{m} = -g \sin \theta$$

When θ is very small.

$$\sin \theta \cong \theta \Rightarrow \therefore a = -g\theta \text{ ----- (2)}$$

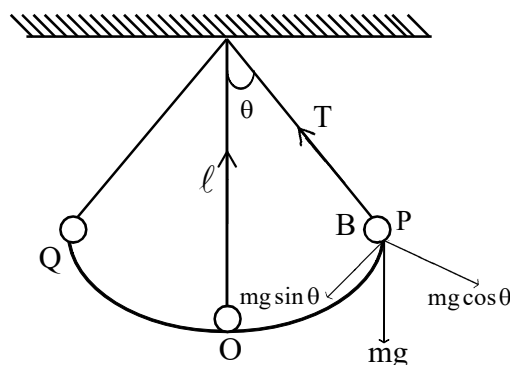
From (1) and (2) eq'n to we get

$$\text{usier S.H.M. } a = -\omega^2 y \text{ ----- (4)}$$

From above eq'n (3) and (4) we, get

$$\text{The work done } = w = \frac{1}{2} m \omega^2 y^2$$

This work done is stored in the



$$a = -g \left(\frac{x}{\ell} \right) \quad \text{-----(3)}$$

-ve sign indicates ' a^H ' and ' θ ' are in opposite directions.

$$\text{Time period : } T = 2\pi \sqrt{\frac{\text{displacement}}{\text{acceleration}}} = 2\pi \sqrt{\frac{x}{a}}$$

$$T = 2\pi \sqrt{\frac{\ell}{g}}$$

Second's Pendulum : A simple pendulum whose time period is 2sec is called as a second's pendulum.

$$T = 2 \text{ sec}$$

3. Derive the eq'n for the K.E and P.E of simple harmonic oscillator and show that total energy of a particle in simple harmonic motion is constant at any point on its path?

Ans:- **Expression for K.E :** The velocity of a particle in S.H.M is given by $v = \omega \sqrt{A^2 - y^2}$

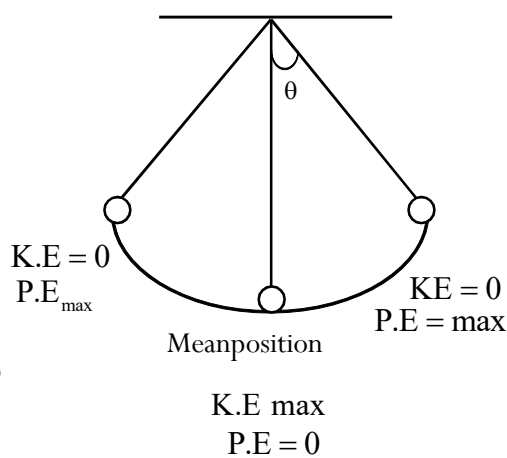
$$\text{K.E} = \frac{1}{2}mv^2 = \frac{1}{2}m\omega^2(A^2 - y^2) \quad \text{-----(1)}$$

we know that $y = A \sin \omega t$

$$\text{K.E} = \frac{1}{2}m\omega^2 A^2 (1 - \sin^2 \omega t) \quad \text{-----(2)}$$

$$\text{when } y = 0, \text{ K.E}_{\max} = \frac{1}{2}m\omega^2 A^2 \text{ (Mean position)}$$

$$\text{when } y = A, \text{ K.E}_{\min} = 0 \text{ (extreme position)}$$



Expression for P.E : When the displacement of a particle executing simple harmonic oscillation increases. The restoring force is in the opposite direction to the displacement therefore work is done in moving through the displacement against restoring force if F is restoring force at the displacement y .

$$\text{The average force against which work is done} = \frac{O + K}{2} = \frac{F}{2}$$

work done displacement = y = average force \times displacement

$$\omega = \frac{F}{2} \times y$$

$$\omega = \frac{m a y}{2} \quad \text{-----(3)}$$

$$\text{from P.E} = \frac{1}{2} m \omega^2 y^2 \quad \text{-----(5)}$$

$$\text{P.E} = \frac{1}{2} m \omega^2 A^2 \sin^2 \omega t \quad \text{-----(6)} \quad (y = A \sin \omega t)$$

$$\text{if } y = 0, \quad \text{P.E}_{\min} = 0 \quad (\text{Mean position})$$

$$y = A \quad \text{P.E}_{\max} = \frac{1}{2} m \omega^2 A^2 \quad (\text{extreme position})$$

Total energy : Total energy = K.E. + P.E.

$$\text{K.E} = \frac{1}{2} m \omega^2 (A^2 - y^2)$$

$$\text{P.E} = \frac{1}{2} m \omega^2 y^2$$

$$\text{T.E} = \frac{1}{2} m \omega^2 (A^2 - y^2) + \frac{1}{2} m \omega^2 y^2$$

$$= \frac{1}{2} m \omega^2 A^2$$

At mean position $y = 0$, $\text{P.E} = 0$

$$\text{K.E}_{\max} = \frac{1}{2} m \omega^2 A^2$$

$$\text{T.E} = \text{K.E} + \text{P.E}$$

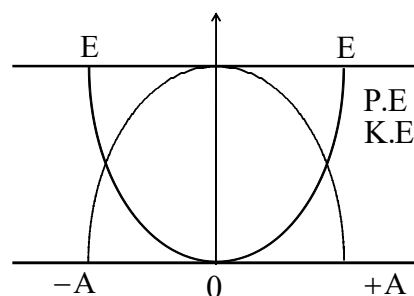
$$\text{T.E} = \frac{1}{2} m \omega^2 A^2 + 0 = \frac{1}{2} m \omega^2 A^2$$

At extreme position $y = A$, $\text{K.E} = 0$ and $\text{P.E}_{\max} = \frac{1}{2} m \omega^2 A^2$

$$\therefore \text{T.E} = \text{K.E} + \text{P.E}$$

$$\text{T.E} = 0 + \frac{1}{2} m \omega^2 A^2 = \frac{1}{2} m \omega^2 A^2$$

From mean position to extreme position K.E is to be converted into P.E.



Problems :

1. A particle executes SHM such that the maximum velocity during the oscillation is numerically equal to half the maximum acceleration what is the time period?

Ans:-

$$V_{\max} = \frac{1}{2} a_{\max}$$

$$A\omega = \frac{1}{2} A \omega^2$$

$$\omega = 2$$

$$T = \frac{2\pi}{\omega} = \frac{2\pi}{2} = \pi \text{ sec}$$

2. A body describes simple harmonic motion with an amplitude of 5 cm and a period of 0.2 sec find the acceleration and velocity of the body when the displacement is (a) 5 cm (b) 3 cm (c) 0 cm.

Ans:- $A = 5\text{ cm} = 5 \times 10^{-2}\text{ m}$ $T = 0.2\text{ sec}$

i) $y = 5\text{ cm} = 5 \times 10^{-2}\text{ m}$ $\omega = \frac{2\pi}{T} = \frac{2\pi}{0.2} = 10\pi$

Acceleration $a = -\omega^2 y \Rightarrow -(10\pi)^2 \times 5 \times 10^{-2}$

$$a = -5\pi^2 \text{ m/s}^2$$

Velocity $V = \omega \sqrt{A^2 - y^2} = 10\pi \sqrt{(5 \times 10^{-2})^2 - (5 \times 10^{-2})^2}$

ii) $y = 3\text{ cm} = 3 \times 10^{-2}\text{ m}$

Acceleration $a = -\omega^2 y = -(10\pi)^2 \times 3 \times 10^{-2} = -3\pi^2 \text{ m/sec}$

velocity $v = \omega \sqrt{A^2 - y^2} = 10\pi \sqrt{(5 \times 10^{-2})^2 - (3 \times 10^{-2})^2}$

$$= 10\pi \sqrt{25 - 9} \times 10^{-2}$$

$$V = 0.4 \pi \text{ m/sec}$$

iii) $y = 0\text{ cm}$ $a = -\omega^2 y = -(10\pi)^2 \times 0 = 0$

Velocity(V) = $\omega \sqrt{A^2 - y^2}$

$$= 10\pi \sqrt{(5 \times 10^{-2})^2 - 0}$$

$$= 0.5 \pi \text{ m/sec}$$

3. A simple harmonic oscillator has a time period of 2s. What will be the change in the phase 0.25 sec after leaving the mean position?

Ans:- $T = 2\text{ sec}$ $t = 0.25\text{ sec}$

$$\sin \omega t = \sin \left(\frac{2\pi}{T} \right) t$$

$$\phi = \omega t = \frac{2\pi}{T} \times t = \frac{2\pi}{2} \times 0.25$$

$$\phi = \frac{\pi}{4}$$

4. On an average a human heart is found to beat 75 times in a minute. Calculate its frequency and period?

Ans:- The beat frequency of heart $= 75/1 \text{ (min)}$

$$= \frac{75}{60} \text{ sec}$$
$$= 1.25 \text{ /sec}$$
$$= 1.25 \text{ Hz}$$

The time period $T = \frac{1}{1.25} \text{ /sec}$

$$T = 0.8 \text{ sec}$$

5. What is the length of a simple pendulum which ticks seconds?

Ans:- $T = 2\pi \sqrt{\frac{L}{g}}$

squaring on both sides.

$$L = \frac{gT^2}{4\pi^2}$$

The time period of a simple pendulum which ticks seconds is 2 sec

$$g = 9.8 \text{ m/s}^2 \quad T = 2 \text{ sec}$$

$$L = \frac{9.8 \times 4}{4 \times (3.14)^2} = 1 \text{ m}$$



UNIT IX

GRAVITATION

VERY SHORT QUESTION & ANSWERS (2 MARKS)

2. State the vector form of Newton's law of gravitation?

Ans:- Vector form of Newton's law of gravitation $F = \frac{Gm_1m_2}{r^3} \hat{r}$

Where \hat{r} is unit vector

3. In the gravitational force of earth on the moon is F, what is the gravitational force of moon on earth? Do these force form an action reaction pair?

Ans:- Yes, they form action and reaction pair.

5. As we go from one planet to another, how will (a) the mass and the weight of a body change?

Ans:- (a) The mass remains constant

(b) The weight ($w=mg$) changes from one planet to another planet.

6. Keeping the length of a simple pendulum constant will the time period be the same on all planets? support your answer with reason?

Ans:- No, Time period depends on acceleration due to gravity (g) $T = 2\pi\sqrt{\frac{L}{g}}$

g values varies from planet to planet. So time period changes..

9. "Hydrogen is in abundance around the sun but not around earth" Explain?

Ans:- The r.m.s velocity of hydrogen molecules at ordinary temperature is around 2 Km S⁻¹, v_e on the sun 620 Km S⁻¹ is greater than v_e on the earth 11.2 KmS⁻¹. The gravitational attraction of the sun is more than the earth. Hence hydrogen is in abundance around the sun and less around the earth.

10. What is the time period of revolution of a geostationary satellite? Does it rotate from west to east or from east to west?

Ans:- Time period of revolution of geostationary satellite is 24 Hrs it rotate from west to east.

11. What are polar satellites?

Ans:- A satellite that revolves in a polar orbit is called a polar satellite. A polar orbit passes over north and south poles of the earth and has a smaller radius 500-800km.

SHORT QUESTION & ANSWERS (4MARKS)

4. What is the orbital velocity? Obtain an expression for it?

Ans:- **Orbital velocity (V_0)** : The horizontal velocity required for an object to revolve around the earth in a circular orbit is called orbital velocity.

Expression for orbital velocity : Consider a body of mass (satellite) m , revolves round the earth in a circular orbit. Let h be the height of the satellite from the surface of the earth. Then $(R+h)$ is the radius of the orbit.

The gravitational force of attraction of the earth on the body is given by

$$F = \frac{GMm}{(R+h)^2} \quad \text{---(1)}$$

The centripetal force on the body is given by $F = \frac{mv_0^2}{(R+h)}$ --- (2)

In order to make the body revolve in the same orbit, its centripetal force must be equal to the gravitational forces.

From eq (1) & (2) $F = \frac{mv_0^2}{(R+h)}$ --- (2)

$$V_0^2 = \frac{GM}{(R+h)}$$

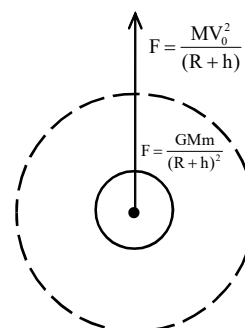
$$V_0 = \sqrt{\frac{GM}{(R+h)}} \quad [\because (R+h) \cong R \text{ if } R \gg h]$$

$$v_0 = \sqrt{\frac{GM}{R}}$$

$$gR^2 = GM$$

$$\Rightarrow v_0 = \sqrt{\frac{gR^2}{R}}$$

$$\boxed{v_0 = \sqrt{gR}}$$



5. What is the escape velocity? obtain an expression for it?

Ans:- **Escape velocity** : It is the minimum velocity with which a body should be projected, so that it moves into the space by overcoming the earth's gravitational field.

Expression for escape velocity :-

Consider a body of mass m thrown with a velocity v_e then $K.E = \frac{1}{2}mv_e^2$ --- (1)

Gravitational P.E = work done on the body

$$P.E = F \times R = \frac{GMm}{R^2} \times R$$

$$P.E = \frac{GMm}{R^2} \text{ ----- (3)}$$

A body just escapes when its K.E = P.E

$$\frac{1}{2} mve^2 = \frac{GMm}{R}$$

$$v_e = \sqrt{\frac{2GM}{R}}$$

$$\text{but } gR^2 = GM$$

$$\Rightarrow v_e = \sqrt{\frac{2gR^2}{R}}$$

$$v_e = \sqrt{2gR}$$

$$v_e = \sqrt{2} \times \sqrt{gR}$$

$$\boxed{v_e = \sqrt{2} \times v_0}$$

6. What is a geo stationary satellite? State its uses?

Ans:- Geo-stationary satellite : If the period of revolution of an artificial satellite is equal to the period of rotation of earth, then such a satellite is called geo stationary satellite.

Time period of geo stationary satellite is 24 hrs.

uses :

- 1) Study the upper layer of atmosphere
- 2) Forecast changes in atmosphere.
- 3) know the shape and size of the earth.
- 4) identify the minerals and natural resources present inside and on the surface of the earth.
- 5) Transmit the T.V. programmes to distant objects.
- 6) Undertake space research to know about the planets, satellites, comets etc.

8. If a nut becomes loose and gets detached from a satellite revolving around the earth, will it fall down to earth or will it revolve earth? Give reasons for your answer?

Ans:- When a nut is detached from a satellite revolving around the earth. The nut is also moving with the speed of the satellite. As the orbit of a satellite does not depend upon its mass. Hence nut is moving in same orbit under centripetal forces.

10. An object projected with a velocity greater than or equal to 11.2 Km/sec will not return to earth. Explain to reason?

Ans:- The escape velocity on the surface of the earth (v_e) = 11.2 km/sec. Any object projected with the velocity greater than (or) equal to 11.2 km/sec. It will not come back. Because it has overcome the earth's gravitational pull.

So an object have back to earth.

LONG QUESTION & ANSWERS (8MARKS)

1. Define gravitation potential energy and derive an expression for it associated with two particles of masses m_1 and m_2 ?

Ans:- Gravitational potential energy : Gravitational potential energy of a body at a point in a gravitational field of another body is defined as the amount of work done in bringing the given body from infinity to that point with out acceleration.

Equation : Consider a gravitational field due to earth of mass, radius R. The mass of the earth can be supposed to be concentrated at its center O. Let us calculate the gravitational potential energy of the body of mass m placed at point p in the gravitational field. Where $OP = r$ and $r > R$,

Let $OA = x$ and $AB = dx$

The gravitational force on the body at A will be

$$F = \frac{GMm}{x^2} \quad \text{----- (1)}$$

small amount of work done in bringing the body without acceleration through a small distance dx is given by $dw = F \times dx$

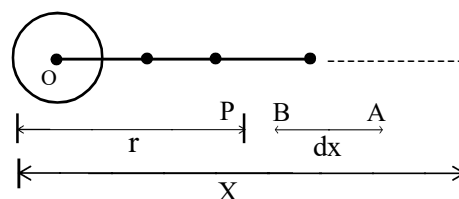
$$dw = \frac{GMm}{x^2} \times dx \quad \text{----- (2)}$$

Total work done in bringing the body from infinity to point p is given by

$$\begin{aligned} w &= \int_{\infty}^r \frac{GMm}{x^2} dx = GMm \int_{\infty}^r x^{-2} dx \\ &= -GMm \left(\frac{1}{x} \right)_{\infty}^r \\ &= \frac{-GMm}{r} \quad \left[\because \frac{1}{\infty} = 0 \right] \\ w &= \frac{-GMm}{r} \quad \text{----- (3)} \end{aligned}$$

This work done is stored in the body as its gravitational potential energy

$$(U) = \frac{-GMm}{r} \quad \text{----- (4)}$$



\therefore Gravitational potential energy associated with two particles of masses m_1 and m_2 separated by a distance r is given by

$$P.E = U = \frac{-G m_1 m_2}{r}$$

Problems :

- Two spherical balls each of mass 1kg are placed 1 km apart. Find the gravitational force of attraction between them?

Ans:- $m_1 = m_2 = 1\text{kg}$ $d = 1\text{km} = 1 \times 10^{-3}\text{m}$

$$F = \frac{G m_1 m_2}{d^2} = \frac{6.67 \times 10^{-11} \times 1 \times 1}{[10^{-3}]^2} = 6.67 \times 10^{-7}\text{N}$$

- The mass of a ball is four times the mass of another ball. When these balls are separated by a distance of 10 cm, the force of gravitation between them is $6.67 \times 10^{-7}\text{N}$. Find the masses of the two balls.

Ans:- $m_1 = m_2 = 4m$, $d = 10\text{m} = 10 \times 10^{-2}\text{m}$ $F = 6.67 \times 10^{-7}\text{N}$

$$F = \frac{G m_1 m_2}{d^2} \Rightarrow 6.67 \times 10^{-7} = \frac{6.67 \times 10^{-11} \times m \times 4m}{[10 \times 10^{-2}]^2}$$

$$4m^2 = 10^2$$

$$m^2 = \frac{100}{4} = 25$$

$$m_1 = m = 5\text{kg}$$

$$m_2 = 4 \times 5 = 4 \times 5 = 20\text{kg}$$

- At a certain height above the earth's surface, the acceleration due to gravity is 4% of its value at the surface of earth. Determine the height.

Ans:- $g_h = 4\%$, $g = \frac{4}{100}g$, $R = 6400\text{km}$

$$g_h = \frac{g}{\left(1 + \frac{h}{R}\right)^2} \Rightarrow \frac{4g}{100} = \frac{g}{\left(1 + \frac{h}{R}\right)^2} \Rightarrow \left(1 + \frac{h}{R}\right)^2 = \frac{100}{4} = 25$$

$$1 + \frac{h}{R} = 5$$

$$\frac{h}{R} = 4$$

$$\Rightarrow h = 4R$$

$$\therefore h = 4R = 4 \times 6400 = 25,600\text{ km}$$

4. A satellite orbits the earth at a height equal to the radius of earth. Find its i) orbital speed and (ii) period of revolution?

Ans:- $h = R$

$$\begin{aligned} \text{i) } v_0 &= \sqrt{\frac{GM}{(R+h)}} = \sqrt{\frac{GM}{(R+R)}} = \sqrt{\frac{GM}{2R}} = \sqrt{\frac{6.67 \times 10^{-11} \times 6 \times 10^{24}}{2 \times 6400 \times 10^3}} \\ &= \sqrt{0.3216 \times 10^8} \\ &= 0.5592 \text{ m/sec} \\ v_0 &= 5.592 \text{ km/sec} \end{aligned}$$

$$\begin{aligned} \text{ii) Time period } T &= \frac{2\pi(R+h)}{v_0} = \frac{2\pi(2R)}{v_0} \\ &= \frac{4 \times 3.14 \times 2 \times 6400 \times 10^3}{5.592} \\ &= 14374.8 = 1.44 \times 10^4 \text{ sec} \\ T &= 4 \text{ Hrs.} \end{aligned}$$

5. A satellite is revolving round in a circular orbit with a speed of 8 km/sec at a height where the value of acceleration due to gravity is 8 m/sec². How high is the satellite from the earth surface? ($R=6000\text{km}$)

Ans:- $v_0 = 8 \text{ km/sec} = 8000 \text{ m/s}$, $g_h = 8 \text{ m/s}^2$, $R = 6000 \times 10^3 \text{ m}$

$$\therefore v_0 = \sqrt{\frac{GM}{R+h}} = \sqrt{g(R+h)}$$

$$v_0^2 = \sqrt{g(R+h)} \Rightarrow (8000)^2 = 8(6000 \times 10^3 + h)$$

$$8 \times 10^6 = 6 \times 10^6 + h$$

$$h = (8 - 6) \times 10^6$$

$$h = 2000 \text{ km}$$



UNIT**X****MECHANICAL PROPERTIES
OF SOLIDS****VERY SHORT QUESTION & ANSWERS (2 MARKS)****1. State Hooke's law of elasticity?**

Ans:- With in the elastic limit stress directly proportional to the strain.

Stress \propto strain

$$\text{Stress} = k \cdot \text{strain} \quad \Rightarrow \quad K = \frac{\text{stress}}{\text{strain}}$$

Where K is modulus of elasticity.

2. State the units and dimensions of stress.

Ans:- i) $\text{Stress} = \frac{\text{Force}}{\text{Area}} = \frac{F}{A}$

S.I units $\rightarrow \text{N} / \text{m}^2$ (or) pascal

ii) Dimensional formula

$$\text{stress} = \frac{MLT^{-2}}{L^2} = [ML^{-1}T^{-2}]$$

3. State the units and dimensions of modulus of elasticity?

Ans:- Modulus of elasticity (k) = $\frac{\text{Stress}}{\text{Strain}}$

units $\rightarrow \text{N} / \text{m}^2$ (or) pascal

Dimensional formula $\rightarrow [ML^{-1}T^{-2}]$

units $\rightarrow \text{N} / \text{m}^2$ (or) pascal

4. State the units and dimensions of young's modulus.

Ans:- Young's modulus (y) = $\frac{\text{Longitudinal stress}}{\text{Longitudinal strain}} = \frac{F / A}{e / L}$

units $\rightarrow \text{N} / \text{m}^2$ (or) pascal

Dimensional formula $\rightarrow [ML^{-1}T^{-2}]$

6. State the units and dimensions of bulk modulus.

Ans:- Bulk modulus (B) = $\frac{\text{Bulk stress}}{\text{Bulk strain}} = \frac{-pV}{\Delta V}$

units $\rightarrow \text{N} / \text{m}^2$ (or) pascal

Dimensional formula $\rightarrow [ML^{-1}T^{-2}]$

7. State the examples of nearly perfect and plastic bodies.

Ans:- Nearly perfect elastic bodies are quartz fibre.

Nearly perfect plastic bodies are dough and clay.

SHORT QUESTION & ANSWERS (4MARKS)

1. Define Hooke's law of elasticity, proportionality, permanent set and breaking stress.

Ans:- **Hooke's law** : "Within the elastic limit stress is directly proportional to the strain

$$\text{stress} \propto \text{strain}$$

$$\text{stress} = k \cdot \text{strain}$$

where k is modulus of elasticity.

Proportionality limit : The maximum stress developed in a body till it obeys Hooke's law is called proportionality limit.

Permanent set : Permanent deformation produced when a body is stretched beyond its elastic limit.

Breaking stress : The maximum stress a body can bear before it breaks.

4. Define stress and explain the types of stress.

Ans:- **Stress** : The restoring force per unit area is called stress.

$$\text{Stress} = \frac{\text{Restoring force}}{\text{Area}} = \frac{F}{A}$$

Stress is classified into three types. (1) Longitudinal stress

(2) Volume (or) Bulk stress (3) Tangential (or) Shearing stress

(1) **Longitudinal stress (or) Linear stress** : When a normal stress changes the length of a body then it is called Longitudinal stress.

$$\text{Longitudinal stress} = \frac{F}{A}$$

(2) **Volume (or) Bulk stress** : When a normal stress changes the volume of a body, then it is called volume stress.

$$\text{Volume stress} = \frac{\text{Force}}{\text{Area}} = \text{Pressure}$$

(3) **Tangential (or) shearing stress** : When the stress is tangential to the surface due to the application of forces parallel to the surface, then the stress is called tangential stress.

$$\text{Tangential stress} = F/A$$

5. Define strain and explain the types of strain.

Ans:- **Strain** : It is the ratio of change in dimension to its original dimension.

$$\text{Strain} = \frac{\text{Changes in dimension}}{\text{original dimension}}$$

strain is of three types.

1. **Longitudinal strain** : It is the ratio of change in length to its original length.

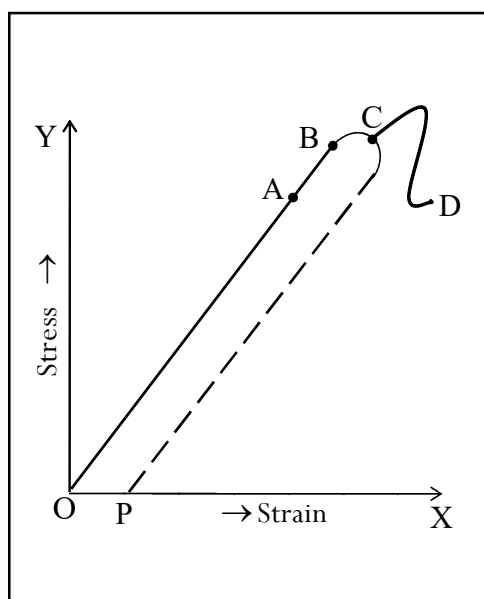
$$\text{Longitudinal strain} = \frac{\text{Changes in length}}{\text{original length}} = \frac{e}{L}$$

2. **Shearing strain (or) Tangential strain** : When simultaneous compression and extension in mutually perpendicular direction takes place in a body, the change of shape it undergoes is called shearing strain.

$$\text{Shearing strain } (\theta) = \ell L.$$

3. **Bulk (or) volume strain** : It is the ratio of change in volume to its original volume is called bulk strain. It is called Bulk (or) volume strain.

$$\text{Bulk strain} = \frac{\text{Change in volume}}{\text{original volume}} = \frac{\Delta v}{v}$$



7. **Explain why steel is preferred to copper, brass, aluminium in heavy-duty machines and in structural designs.**

Ans:- The elastic behavior of materials plays an important role in everyday life. Designing of buildings, the structural design of the columns, beams and supports require knowledge of strength of material used.

The elasticity of the material is due to stress developed within the body, when external force acts on it. A material is of more elastic nature if it develops more stress (or) restoring force. Steel develops more stress than copper, brass, Aluminium for same strain. So steel is more elastic.

$$y = \frac{\text{stress}}{\text{strain}}$$

8. **Describe the behaviour of a wire under gradually increasing load.**

Ans:- When the load is increased in steps, a graph is drawn between stress on y-axis and corresponding strain on x-axis.

- (1) **Proportionality limit** : In the linear position OA, stress is proportional to strain i.e. Hooke's law is obeyed by the wire up to point A.

The graph is a straight line. When ever the wire regains its original length.

A is called proportionality limit.

- (2) **Elastic limit** : In the graph B is the elastic limit. Through the wire does not obey Hooke's law at B. The wire regains its original length after removing the stretching force at B. Up to point B the wire is under elastic behaviour.

- (3) **Permanent set (or) yield point :** In the graph C is the yield point. If the stretching force at C is removed, the wire does not regain its original length and the length of the wire changes permanently. In this position the wire flows like a viscous liquid. After the point C, the wire is under plastic behaviour. C is called permanent set (or) yield point.
- (4) **Breaking point :** When the stress increased, the wire becomes thinner and thinner and thinner when the stress increases to a certain limit the wire breaks. The stress at which the wire breaks is called breaking stress and the point D is called breaking point.
- (5) **Elastic fatigue :** The state of temporary loss of elastic nature of a body due to continuous strain is called elastic fatigue. When a body is subjected to continuous strain within the elastic limit, it appears to have lost elastic property temporarily to some extent and becomes weak.

Problems :

1. **A copper wire of 1mm diameter is stretched by applying a force of 10N. Find the stress in the wire.**

Ans:- $D = 1\text{mm} = 10^{-3}$, $r = D/2 = 0.5 \times 10^{-3}\text{m}$

$F = 10\text{N}$

$$\text{stress} = \frac{F}{A} = \frac{F}{\pi r^2}$$

$$= \frac{10}{3.14 \times (0.5 \times 10^{-3})^2} = 1.273 \times 10^7 \text{ N/m}^2$$

2. **A tungsten wire of length 20 cm is stretched by 0.1cm. Find the strain on the wire.**

Ans:- $L = 20 \times 10^{-2}\text{m}$, $\Delta L = 0.1 \times 10^{-2}\text{m}$

$$\text{strain} = \frac{\Delta L}{L} = \frac{0.1 \times 10^{-2}}{20 \times 10^{-2}} = 0.005$$

3. **If an iron wire is stretched by 1%, What is the strain on the wire?**

Ans:- $\text{Strain} = \frac{\Delta L}{L} = 1\%$

$$= \frac{1}{100} = 0.01$$

4. Determine the pressure required to reduce the given volume of water by 2%.
Bulk modulus of water is $2.2 \times 10^9 \text{ Nm}^{-2}$.

$$\text{Ans:- } \frac{-\Delta v}{v} = 2\% = \frac{2}{100}$$

$$B = 2.2 \times 10^9 \text{ N / m}^2$$

$$B = \frac{-Pv}{\Delta v}$$

$$P = -B \times \frac{\Delta v}{v}$$

$$= 2.2 \times 10^9 \times \frac{2}{100}$$

$$P = 4.4 \times 10^7 \text{ N / m}^2$$



UNIT XI

MECHANICAL PROPERTIES OF FLUIDS

VERY SHORT QUESTION & ANSWERS (2 MARKS)

1. Define average pressure, mention it's units and dimensional formula?

Ans:- Average pressure is defined as the normal force acting per unit area.

$$P_{ave} = \frac{F}{A} = \frac{\text{Force}}{\text{Unit Area}}$$

$$\text{Units : } \frac{\text{N}}{\text{m}^2} \text{ (or) pascals}$$

$$\text{Dimensional formula : } ML^{-1}T^{-2}$$

2. Define viscosity. What are units and dimension formula?

Ans:- The property of a liquid which opposes the relative motion between its two layers is called viscosity.

$$\text{Units : } \frac{\text{N-S}}{\text{m}^2} \text{ (or) pascals - sec.}$$

$$\text{Dimensional formula : } ML^{-1}T^{-1}$$

3. Why are water drops and bubbles in spherical shape?

Ans:- Due to surface tension. The surface tension of a liquid tends to have minimum surface area. The spherical shape occupies minimum surface area while comparing other shapes. So rain drops are always spherical shape.

4. Which instruments are used by the principle of venturi meter?

Ans:- Carburetor of automobile, Aspirators, Bunsenburner, Atomisers, Filterpumps, Sprayers are used on this venturi meter principles.

5. What is angle of contact?

Ans:- The angle between tangent to the liquid surface at the point of contact and solid surface inside the liquid is termed as angle of contact (θ).

6. What is magnus effect?

Ans:- The difference in the velocities of air results in the pressure difference between the lower and upper faces. and there is a net upward force on the ball. This dynamic lift due to spinning is called "magnus effect".

7. Give the expression for the excess pressure in a liquid drop?

$$\text{Ans:- Excess pressure in a liquid drop } P_i - P_o = \frac{2s}{r}$$

Here S = Surface tension

r = Radius of the liquid drop.

8. Give the expression for the excess pressure in an air bubble inside the liquid?

Ans:- Excess pressure in an air bubble inside the

$$\text{liquid } P_i - P_o = \frac{2s}{r}$$

Here S = Surface tension

r = Radius of the liquid drop.

9. Give the expression for excess pressure of the soap bubble in air?

Ans:- Soap bubble have two interfaces, hence excess pressure inside a soap bubble is

$$P_i - P_o = \frac{4S}{r}$$

Where S = Surface tension

r = radius of the soap bubble.

10. What is Reynolds number?

Ans:- Reynold number is a pure number which determines the nature of fluid flow. 'R' is the Reynold number.

$Re < 1000$ to stream line flow

$Re > 2000$ to turbulent flow

$1000 < Re < 2000$ to unsteady flow

SHORT QUESTION & ANSWERS (4MARKS)

1. What is atmospheric pressure and how it is determined using Barometer?

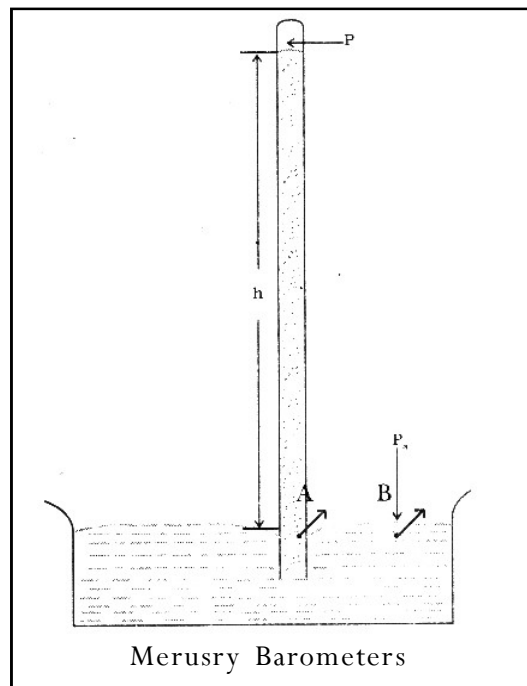
Ans:- **Atmospheric pressure :** Atmospheric pressure at any point is equal to the weight of a column of air of the top of the earth's atmosphere.

$$1 \text{ atm} = 1.013 \times 10^5 \text{ pa}$$

Determination of atm pressure using Barometer

: A long glass tube closed at one end and filled with mercury is inverted in to a trough of mercury. This device is known as mercury barometer.

The space above the mercury column in the tube contains only mercury vapour whose pressure 'p' is so small, that it may be neglected. The pressure inside the column at 'A' must equal the pressure at 'B'



\therefore Pressure at 'B' = Atmospheric pressure = P_a

$P_a = pgh$ = pressure at 'A'

Where 'p' is density of mercury and 'h' is the height of the mercury column in the tube. In the experiment it is found that the mercury column in the barometer has a height of about 76 cm at the sea level equivalent to one atmosphere.

2. State pascal's law and verify it with the help of an experiment?

Ans:- **Pascal law** : It states that if gravity effect is neglected. The pressure at every point equilibrium of rest is same.

Proof:

- Imagine a circular cylinder of uniform cross sectional area 'A'. Such that points 'C' and 'D' lies on flat faces of the cylinder.
- The liquid inside the cylinder in equilibrium under the action of force exerted by the liquid outside the cylinder.
- Thus the forces on the flat faces of the cylinder at 'C' and 'D' will be perpendicular to the forces on the curved surface of the cylinder.
- Since liquid is in equilibrium. The sum of the forces acting on the curved surface of the cylinder must be zero.
- If P_1 and P_2 are the pressures at point 'C' and 'D' respectively F_1 and F_2 are the forces acting on the flat surface of the cylinder due to liquid, then $F_1 = P_1 A$

$$F_2 = P_2 A$$

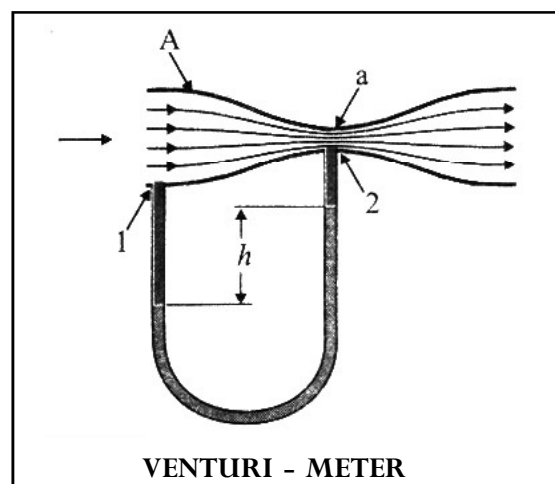
liquid is in equilibrium, therefore $F_1 = F_2$

$$P_1 A = P_2 A \Rightarrow \boxed{P_1 = P_2}$$

3. What is venturi - meter? Explain how it is used?

Ans:- Venturi meter : The venturi - meter is a device to measure the flow speed of incompressible fluid.

- It consists of a tube with a broad diameter and small constriction at the middle.
- A manometer in the form of a U-tube is also attached to it, with one of arm at the broad neck point of the tube and the other constriction as shown in figure.
- The manometer contains a liquid of density 'p'.



- The pressure difference causes the fluid in the U-tube connected at the narrow neck to rise in comparison to the other arm.
- Filter pumps, sprayers used for perfumes, carburetor of automobile has used on this principle.

4. Explain surface Tension and surface Energy?

Ans:- The force acting per unit length of an imaginary line drawn on the surface of liquid, normal to it and parallel to the surface is called surface tension.

$$T = \frac{F}{l} \quad \text{units : N/m} \quad \text{D.F : } ML^0 T^{-2}$$

Surface energy (E) : The additional potential energy due to molecular forces per unit surface area is called surface energy.

$$\text{S. energy (E)} = \frac{\text{Workdone}}{\text{Area}} \quad \text{units : J/m}^2 \quad \text{D.F : } MT^{-2} L^0$$

LONG QUESTION & ANSWERS (8MARKS)

1. State Bernoulli's principle from conservation of energy in a fluid flow through a tube, arrive at Bernoulli's equation?

Ans:- **Bernoulli's principle :-** Bernoulli's principle states that in a stream line flow, the sum of the pressure, the K.E per unit volume and the P.E per unit volume remains a constant.

- Consider a non-viscous, incompressible fluid is flowing through the pipe in a steady flow.
- A_1 is cross sectional area at one end of the pipe, and which is h_1 height from the ground level.
- A_2 is cross sectional area at second end of the pipe and which is h_2 height from the ground level.

where $h_1 > h_2$.

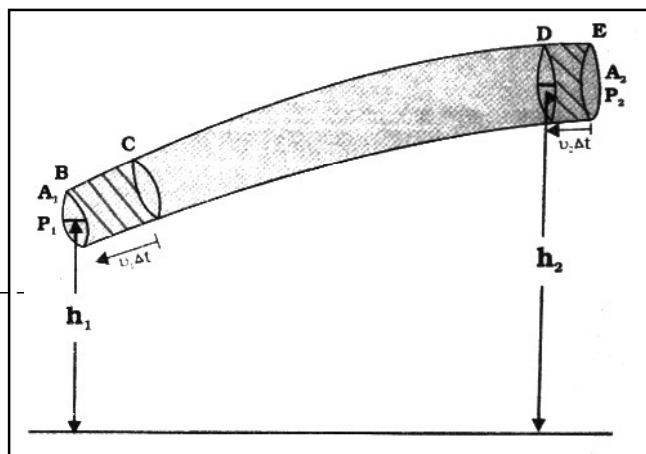
- During short time interval this fluid would have moved v_1 is the speed at first end and v_2 is the speed at second end. But density ' ρ ' is same at both ends.
- P_1 P_2 are the pressures respectively.

According to the equation of continuity the mass of the liquid entering the tube equal to the mass of the liquid flowing through the tube.

$$\therefore P_1 A_1 V_1 dt = P_2 A_2 V_2 dt$$

Here mass of the liquid at first end is $P_1 A_1 V_1 dt$

mass of the liquid at second end is $P_2 A_2 V_2 dt$



Where $f_1 = f_2$ as the fluid is incompressible

$$\text{from eqn (1) } A_1 V_1 = A_2 V_2 \quad \text{-----(2)}$$

The workdone on the fluid in the tube as the fluid enters the tube through first end is $P_1 V_1 A_1 dt$,

and the work done by the fluid as it comes out of the tube through second end is $P_2 V_2 A_2 dt$.

$$\text{The total workdone on the fluid} = P_1 V_1 A_1 dt - P_2 V_2 A_2 dt \quad \text{-----(3)}$$

The total workdone by the gravitational force on the fluid,

as the fluid falls from the heights h_1 to h_2

$$\therefore w_g = m(h_1 - h_2)g \quad \text{-----(4)}$$

The total workdone on the fluid $= w_p + w_g$

According to work energy theorem, the workdone on the fluid is equal to the change in K.E of the fluid.

Hence

$$P_1 A_1 V_1 dt - P_2 A_2 V_2 dt + m(h_1 - h_2)g = \frac{1}{2} (v_2^2 - v_1^2) m \quad \text{-----(6)}$$

dividing B. sides by $m = \rho A_1 V_1 dt = \rho A_2 V_2 dt$

$$\frac{P_1}{\rho} + h_1 g + \frac{1}{2} v_1^2 = \frac{P_2}{\rho} + h_2 g + \frac{1}{2} v_2^2$$

$$\therefore \boxed{\frac{P}{\rho} + hg + \frac{1}{2} v^2 = \text{constant}}$$

The above eqn expressed as Bernoulli's eqns.

Applications :

1. When the forced wind flows on the top of the houses, which are lifted up due to dynamic lift on the roofs.
2. Small pieces of paper on the table, which are disturbed due to fan air.

Problems :

1. Diameter of the soap bubble 0.6cm. Find the work done against displacement of bubble due to surface tensional force?

$$\text{Ans:- } D = 0.6\text{cm} = 0.6 \times 10^{-2}\text{m}$$

$$r = \frac{D}{2} = \frac{0.6 \times 10^{-2}}{2} = 0.3 \times 10^{-2}\text{m}$$

$$\delta = 2.5 \times 10^{-2} \text{ N/m}$$

$$w = 8\pi r^2 s$$

$$= 8 \times 3.14 \times (0.3 \times 10^{-2})^2 \times 2.5 \times 10^{-2}$$

$$w = 5.652 \times 10^{-6} \text{ J}$$

2. Capillary tube is dipped in water capillary rises 6cm high, what is its radius of capillary tube? (S.T of water = $7.2 \times 10^{-2} \text{ N/m}$)

Ans:- $h = 6 \times 10^{-2} \text{ m}$, $\delta = 7.2 \times 10^{-2} \text{ N/m}$

Density of water $\rho = 10^3 \text{ kg/m}^3$

$$\delta = \frac{h\rho g r}{2}$$

$$r = \frac{2\delta}{h\rho g} = \frac{2 \times 7.2 \times 10^{-2}}{6 \times 10^{-2} \times 10^3 \times 9.8}$$

$$r = \frac{14.4}{58.8} \times 10^{-3}$$

$$r = 0.24 \times 10^{-3} \text{ m} \Rightarrow 0.24 \text{ mm}$$

3. Work done 'w' by the preparation of bubble w.r. to 'R' radius. How much energy required to its radius double of bubble?

Ans:- $R_1 = R$ $R_2 = 2R$

Initial work $(w) = 8\pi R^2 s$

Final work $(w^1) = 8\pi [R_2^2 - R_1^2] s$

$$= 8\pi [4R^2 - R^2] s$$

$$= 3 \times 8\pi R^2 s$$

$$\boxed{w^1 = 3w}$$



UNIT XII

THERMAL PROPERTIES OF MATTER

VERY SHORT QUESTION & ANSWERS (2 MARKS)

1. Distinguish between heat and temperature?

Ans:-

Heat

- 1) Transforms the energy due to different temperatures of the two systems is called 'heat'.
- 2) It is measured in joules (or) calories
- 3) It is determined with calorimeter

Temperature

- 1) It is a degree of hotness (or) coldness of a body is called temperature.
- 2) It is measured centigrade (or) fahrenheit.
- 3) It is measured with thermometer.

2. If substance contract on heating? Give an example?

Ans:- Yes, rubber, type metal, cast iron, such substances contract on heating.

3. Why gap are left between rails on a railway track?

Ans:- The length of the railway track increases in summer due to high temperature. Therefore a gap is left to allow this expansion.

4. What is latent heat of fusion?

Ans:- The amount of heat per unit mass required to change a substance from solid into liquid at the same temperature and pressure is called the latent heat of fusion.

5. What is latent heat of vapourisation?

Ans:- The amount of heat per unit mass required to change a substance from the liquid to the vapour state at the same temperature and pressure is called the latent heat of vaporisation.

6. What is specific gas constant? units and D.F?

Ans:- It is defined as the constant per unit mass.

$$r = \frac{R}{M}$$

units : J kg⁻¹ K⁻¹

D.F : L² T⁻² K⁻¹

7. Why utensils are coated black? Why the bottom of the utensils are made of copper?

Ans:- - Utensils are coated black, because it is a good absorber of heat.

- Copper is a good conductor of heat, so copper is used at the bottom of cooking utensils.

8. State weins displacement law?

Ans:- The wave length (λ_m) corresponding to manimum energy emitted by a black body is inversely propertional to its absolute temperature (T).

$$\text{i.e } \lambda_m \propto \frac{1}{T}$$

10. What is green house effect? Explain glocal warming?

Ans:- Green house effect : when the earth recieves sun light. It gets heated up and emits infrared, CH_4 , N_2O , O_3 , chlorofluro carbon (green house gases) present in the air absorbs the heat content of infrared radiation and keeps the earth warm, This is called green house effect.

Global worming : As CO_2 content increases, more heat is retained in the atmosphere and the temperatures all over the world increases. This is called global warming.

11. Define absorptive power of a body. What is the absorpture power of a perfect black body?

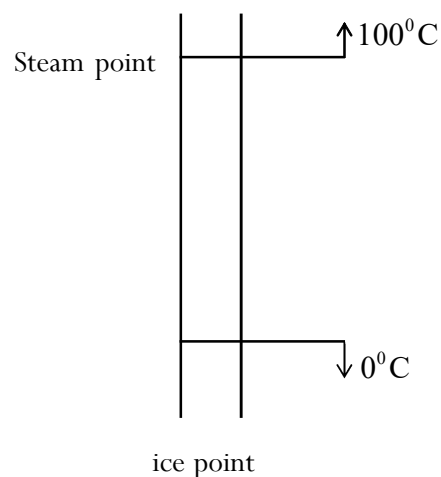
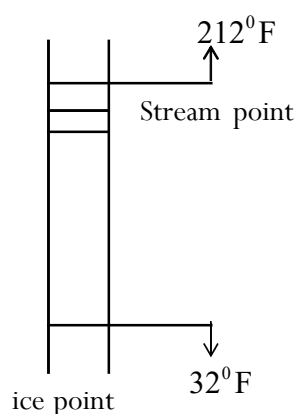
Ans:- Absorptive power : At given temperature and wave length, the ratio of the amount of radiant energy absorbed to the amount of radiant energy incident in a wave length range is called the absorptive power at that temperature and wavelength.

\therefore Absorptive power of a perfect black body is 1.

SHORT QUESTION & ANSWERS (4MARKS)**1. Explain celrius and Fahren hit scales of temperatures, obtain the selation between celain, fahran heit and kelving scales of temperatures?**

Ans:- **Centingrade scale of temperature** : In this scale the lower fixed point is called the ice point and is assigned the value 0°C . The upper fined point is called the steam point and is assigned the value 100°C . The interval between these two points ($100^\circ\text{C} - 0^\circ\text{C} = 100^\circ\text{C}$) is subdivided in to 100 equal parts each one corsesponding to 1°C .

Fahrenheit scale of temperature : In the fahrenheit scale of temp the lower fixed point is the ice point and is assigned a value 32°F and the upper fixed point is the steem point and is assigned a value 212°F . The interval between these two points ($212^\circ\text{F} - 32^\circ\text{F} = 180^\circ\text{F}$) is subdivided into 180 equal parts each one cosresponding to 1°F .



Relation :
$$\frac{C}{100} = \frac{F - 32}{180} = \frac{K - 273}{100}$$

C & F relation :
$$\frac{C}{100} = \frac{F - 32}{180}$$

$$\frac{C}{5} = \frac{F - 32}{9}$$

$$C = \frac{5}{9} (F - 32) \quad (\text{or}) \quad F = \frac{9C}{5} + 32$$

2. State Newton's law of cooling. What are the conditions for applicable Newton's law of cooling?

Ans:- The state of loss of heat is directly proportional to the difference in temperature between the body and its surroundings provided the temperature difference is small.

i.e.
$$-\frac{dQ}{dt} \propto (T_2 - T_1)$$

$$-\frac{dQ}{dt} = K(T - T_0)$$

Here K = Proportional constant

T = Temperature of object

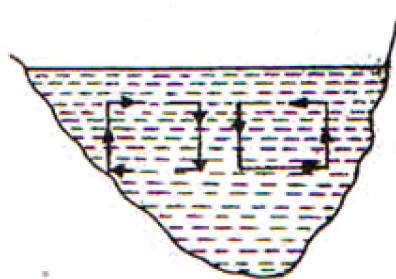
T_0 = Surrounding temperature.

Applicable conditions :

- Loss of heat is negligible by conduction and only when it is due to convection.
- Temperature of the body is uniformly distributed over it.
- Temperature differences are moderate i.e. up to 30K.
- Loss of heat occurs in stream lined flow of air i.e. forced convection.

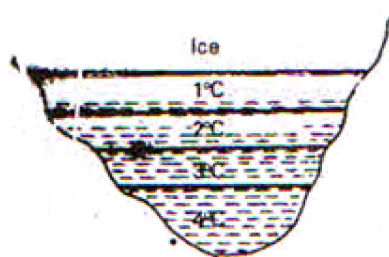
3. In what way is the anomalous behaviour of water advantageous to aquatic animals?

Ans:- In cold countries, as atmospheric temperature decreases, the upper layers of the lakes rivers etc cool, contract and sink to the bottom. This goes on until the whole of the water reaches the temperature of 4°C . When the top layers cool further temperature falls below 4°C it expands and becomes lighter. It does not sink down wards and remains at the top with further cooling the top layer gradually forms ice at the top. Ice and water are bad conductors of heat.



Expansion of water moves upper

to lower and lower to upper.



Formation of ice at the top

with water below.

So the lower layers are protected against freezing by the layers of ice and cold water at 1°C , 2°C and 3°C . This results in water remaining at the bottom at 4°C . So that aquatic animals survive in those layers of water.

LONG QUESTION & ANSWERS (8MARKS)

1. State Boyle's law and Charles's law derive ideal gas equation?

Ans:- **Boyle's law** : The volume of a given mass of gas is inversely proportional to its pressure at constant temperature.

$$\text{i.e } V \propto \frac{1}{P} \text{ (at const. temp)}$$

$$\boxed{PV = \text{Constant}}$$

Charles's law : a) The volume of a given mass of gas is directly proportional to its absolute temperature at constant pressure.

$$\text{i.e } V \propto T \text{ (at const pressure)}$$

$$\boxed{\frac{V}{T} = \text{Constant}}$$

b) The pressure of a given mass of gas is directly proportional to its absolute temperature at constant volume.

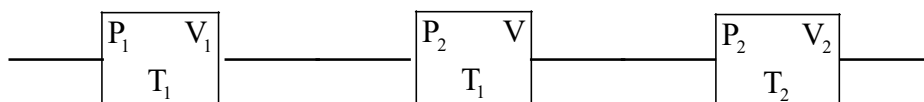
$$\text{i.e } P \propto T \text{ (at const. volume)}$$

$$\boxed{\frac{P}{T} = \text{Constant}}$$

Ideal gas equation : Consider a given mass of gas having a volume V_1 at a pressure P_1 and absolute temperature T_1 . When the temperature changed to T_2 . Let the gas occupies a volume V_2 at a pressure ' P_2 '.

Let this change takes place in two steps.

i) At constant temperature T_1 pressure of the gas changes P_1 to P_2 then volume changes V_1 to ' V '.



according boyle's law $P_1 V_1 = P_2 V \Rightarrow V = \frac{P_1 V_1}{P_2}$ ----- (1)

ii) Let constant pressure P_2 , Absolute temperature changes T_1 to T_2 than volume of the gas changes V to V_2 .

according to charle's law $\frac{V_1}{T_1} = \frac{V_2}{T_2} \Rightarrow V = \frac{V_2 T_1}{T_2}$ ----- (2)

Comparing eqn (1) & (2)

$$\frac{P_1 V_1}{P_2} = \frac{V_2 T_1}{T_2}$$

$$\Rightarrow \frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2}$$

$$\Rightarrow \frac{PV}{T} = \text{Constant (R)} (\because R \text{ ideal gas constant})$$

$$\boxed{PV = RT} \text{ for 1 mole of gas.}$$

Problems :

1. At what temperature kelvin reading and farin heit readings are eqeal?

Ans:- The relation between kelvin scales and fahrein heit

$$\text{scale is } \frac{K - 273.15}{100} = \frac{P - 32}{180}$$

$$\text{But } K = F$$

$$\frac{F - 273.15}{100} = \frac{F - 32}{180}$$

$$F - 273.15 = \frac{5}{9}F - \frac{160}{9}$$

$$F - \frac{5}{9}F = 273.15 - \frac{160}{9} = 273.15 - 17.77$$

$$\frac{4F}{9} = 255.38$$

$$\therefore F = \frac{9}{4} (255.38) = 574.6^\circ\text{F}$$

2. **Length of the aluminium rod rises to 1% then what is the increasing temperature requires? ($\alpha = 25 \times 10^{-6} / ^\circ\text{C}$)**

Ans:- Percentage of increasing length $= \frac{\ell_2 - \ell_1}{\ell_1} \times 100$

$$= \alpha (t_2 - t_1) \times 100 \quad \text{----- (1)}$$

$$\left[\because \frac{\ell_2 - \ell_1}{\ell_1} = \alpha (t_2 - t_1) \right]$$

Here 1% in increasing in length

$$\alpha = 25 \times 10^{-6} / ^\circ\text{C}$$

From eqn (1) $\therefore 1 = 25 \times 10^{-6} (t_2 - t_1) \times 100$

$$t_2 - t_1 = \frac{1}{25 \times 10^{-4}} = \frac{10^4}{25} = 400^\circ\text{C}$$

3. **37°C Temperature, 75cm mercury level pressure at specific mass, volume of gas is 620CC, find the volume at N.T.P?**

Ans:- Here $P_1 = 75 \text{ cm of Hg}$ $V_1 = 620 \text{ CC}$

$$T_1 = 37 + 273 = 310\text{K}$$

at NTP $P_2 = 76 \text{ cm of Hg}$, $T_2 = 273\text{K}$

$$V_2 = ?$$

$$\frac{P_1 V_1}{T_1} = \frac{P_2 V_2}{T_2} \Rightarrow V_2 = \frac{P_1 V_1 T_2}{P_2 T_1}$$

$$V_2 = \frac{75 \times 620 \times 273}{76 \times 310} = 538.8 \text{ CC}$$

4. **14kg mass of Nitrogen volume is 0.4m³ at 30°C temperature then find the pressure?**

Ans:- Mass of the gas (m) = 14kg

$$= 14 \times 10^3 \text{ gm}$$

atomic weight of $N_2 = 28$

$$V = 0.4\text{m}^3 : T = 30^\circ + 273 = 303\text{K}$$

$$PV = nRT = \frac{m}{M} RT$$

$$P = \frac{m}{M} \frac{RT}{V}$$

$$= \frac{14 \times 10^3 \times 8.317 \times 303}{28 \times 0.4}$$

$$\therefore P = 31.5 \times 10^5 \text{ N/m}^2$$

5. A black body maximum radiation intensity is found at 2.65 μm . Then find the temperature of the object emits radiation? (Weins constant = $2.9 \times 10^{-3} \text{ mK}$)

Ans:- $\lambda_{\text{max}} = 2.65 \mu\text{m} = 2.65 \times 10^{-6} \text{ m}$

weins constant (b) = $2.90 \times 10^{-3} \text{ mK}$

$$\lambda_{\text{max}} T = b (\text{Constant})$$

$$T = \frac{b}{\lambda_{\text{max}}} = \frac{2.9 \times 10^{-3}}{2.65 \times 10^{-6}}$$

$$\therefore T = 1094 \text{ K}$$



UNIT XIII

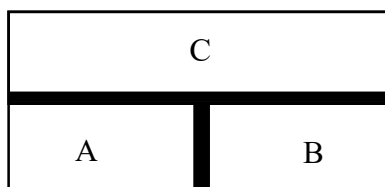
THERMODYNAMICS

VERY SHORT QUESTION & ANSWERS (2 MARKS)

1. Define thermal equilibrium. How does it lead to zero its law of thermodynamics?

Ans:- If the temperatures of the two systems are equal, then they are said to be "thermal equilibrium".

Zeroth law of thermodynamics : If two systems A,B are thermal equilibrium then two systems A, B thermal equilibrium with each other.



2. Define specific heat capacity of the substance?

Ans:- Specific heat capacity : The amount of heat required to raise the 1 gm of substance through 1°C (or) 1K is called specific heat capacity

$$S = \frac{1}{m} \cdot \frac{\Delta Q}{\Delta T} \text{ it depends on nature of the substance and temperature.}$$

4. In summer, when the valve of a bicycle tube is opening the escaping air appears cold, Why?

Ans:- This happens due to adiabatic expansion of the air of the tube of the bicycle.

5. By leaving the door of an electric refrigerator open a room cooled (or) not?

Ans:- No, A room can not be cooled by leaving the door of a refrigerator open. But it will get slightly heated.

6. A Thermos flask containing a liquid is shaken vigorously. What happens to its temperature?

Ans:- Work is done by the liquid on the wall of flask, since it is vigorously shaken. Hence internal energy and temperature of the liquid increases.

7. How much will be the internal energy change in isothermal process, adiabatic process?

- Ans:- - Change in internal energy during isothermal process is $dv = 0$ ($\because U$ is constant)
- But in adiabatic process is two ways.
- ie - during adiabatic compression increases
- during adiabatic expansion decreases.

SHORT QUESTION & ANSWERS (4MARKS)

1. State and explain first law of thermodynamics.

Ans:- The amount of heat supplied to system is equal to the algebraic sum of the change in internal energy of the system and the amount of external work done.

i.e. $\Delta Q = \Delta U + \Delta W$ where ΔQ = amount of heat

ΔU = internal energy

ΔW = External workdone

If is special case of law of conservation of energy.

2. Define two principles of specific heat gas. Which is greater and Why?

Ans:- We have two specific heat of a gases are

(1) molar specific heat capacity at constant pressure (C_p)

(2) Molar specific heat capacity at constant volume (C_v)

(1) C_p : The amount of heat required to raise the temp. of 1 gm mole of a gas through 10°C at constant pressure is called molar specific heat at constant pressures (C_p)

i.e. $C_p = \frac{1}{\mu} \frac{\Delta Q}{\Delta T}$ where ' μ ' is no of moles.

(2) C_v : The amount of heat required to raise the temp of 1gm mole of gas through 1°C at constant volume is called molar specific heat at constant volume (C_v)

i.e. $C_v = \frac{1}{\mu} \frac{\Delta Q}{\Delta T}$

$C_p > C_v$ In C_v system the gas is heated at constant volume, no work is done. therefore the heat is supplied is to be used only in rising the temp.

3. Derive a relation between the two specific heat capacities of gas on the basis of 1st law of thermodynamics.

Ans:- At constant pressure one mole ideal gas acquires amount of heat (dQ) ' du ' is the internal energy raises then external workdone $dw = pdv$.

$\therefore dQ = du + pdv$ -----(1)

According to definition of specific heat at constant volume for 1 mole of gas is

$C_v = \left(\frac{dQ}{dT} \right)_v$ -----(2)

But at constant volume $dV=0$ there fore

from eqn (1) $dQ=dU + P (dV)$

$$dQ = dU$$

$$\text{from eqn (2) } C_v = \left(\frac{dU}{dT} \right)_v \quad (\because dQ = dU) \quad \text{-----(3)}$$

According to definition of specific heat at constant pressure.

$$C_p = \left(\frac{dQ}{dT} \right)_p \quad \text{-----(4)}$$

Differentiate w.r. to temperature either sides of the eqn. (1)

$$\therefore \left(\frac{dQ}{dT} \right)_p = \left(\frac{dU}{dT} \right)_p + p \left(\frac{dV}{dT} \right)_p$$

But internal energy of the ideal gas depends on temp 'T' so bottom indicator 'p' if $\frac{dV}{dT}$ is neglected from the above eqn.

$$\therefore C_p = \left(\frac{dU}{dT} \right)_r + p \left(\frac{dV}{dT} \right)_p \quad (\because \text{from eqn(3)})$$

$$C_p = C_v + p \left(\frac{dV}{dT} \right)_p \quad (\because PV = RT \text{ partial differ})$$

$$C_p = C_v + R \quad P.dv = R.dT$$

$$\boxed{C_p - C_v = R} \quad P \cdot \left(\frac{dV}{dT} \right)_p = R$$

4. Determine the workdone by an ideal gas during isothermal change?

Ans:- Let a certain mass of gas expands from pressure P_1 to P_2 and volume V_1 to V_2 isothermally at constant temperature T.

work done 'dw' volume of gas expands from V_1 to V_2 at constant pressure

$$dw = p dv$$

$$\therefore \text{ total workdone } w = \int_{V_1}^{V_2} dw = \int_{V_1}^{V_2} p.dv \quad \text{-----(1)}$$

In isothermal process $PV=\text{constant}$

$$PV = \mu RT$$

$$P = \frac{\mu RT}{V} \quad \text{Where } \mu = \text{no.of moles}$$

'P' value substitute in eqn (1)

$$\begin{aligned}
 W &= \int_{V_1}^{V_2} \mu \frac{RT}{V} \cdot dV = \mu RT \int_{V_1}^{V_2} \frac{1}{V} \cdot dV \\
 &= \mu RT \log_e [V]_{V_1}^{V_2} \\
 W &= \mu RT \log_e \left(\frac{V_2}{V_1} \right)
 \end{aligned}$$

Total workdone in isothermal process

$$W = 2.3026 RT \log_e \left(\frac{V_2}{V_1} \right)$$

5. Determine the workdone by an ideal gas during adiabatic change?

Ans:- During an adiabatic change the state of an ideal gas changes from (P_1, V_1, T_1) to (P_2, V_2, T_2) . The workdone during a small change in volume dv at constant pressure is $dw = pdr$.

Total workdone by gas from V_1 to V_2 is

$$\text{i.e } W = \int_{V_1}^{V_2} dw = \int_{V_1}^{V_2} p \cdot dr \quad \text{-----(1)}$$

adiabatic relation between pressure and volume

$$PV^2 = \text{constant (K)} \quad \text{-----(2)}$$

$$P = \frac{K}{V^r} \quad \text{-----(3)}$$

$$\text{and } P_1 V_1^2 = P_2 V_2^2 = K$$

Substitute eqn (3) in (1)

$$W = \int_{V_1}^{V_2} p \cdot dV = \int_{V_1}^{V_2} \frac{k}{V^r} \cdot dr$$

$$W = k \left(\frac{V^{1-r}}{1-r} \right)_{V_1}^{V_2}$$

$$W = \left[\frac{K \cdot V_2^{1-r}}{1-r} - \frac{K \cdot V_1^{1-r}}{1-r} \right] = \left[\frac{P_2 V_2^r V_2^{1-r}}{1-r} - \frac{P_1 V_1^r V_1^{1-r}}{1-r} \right]$$

$$W = \frac{1}{1-r} [P_2 V_2 - P_1 V_1]$$

But gas eqn $P_1 V_1 = RT_1$ & $P_2 V_2 = RT_2$

$$W = \frac{1}{1-r} (RT_2 - RT_1)$$

$$\therefore w = \frac{R}{1-\gamma} (T_2 - T_1)$$

6. Distinguish between isothermal and adiabatic process?

Ans:-

Isothermal change

- 1) Changes in P, V and constant temperature.
- 2) Amount of heat changes
- 3) The gas remains in good thermal contact with surroundings and heat is exchanged.
- 4) Here $PV = \text{constant}$
- 5) This process takes place slowly
- 6) Internal energy remains constant $dU=0$.

Adiabatic change

- 1) Changes in P, V of gas and constant heat.
- 2) Temperature changes.
- 3) The gas is isolated from the surroundings and heat is not exchanged.
- 4) Here $PV^\gamma = \text{constant}$
- 5) This process takes place quickly
- 6) Entropy is constant.

7. Explain the cyclic process and Non cyclic process?

Ans:-

1) Cyclic process : A process in which the system after passing through various stages like pressure, volume, temp changes, returns to its initial stage is called cyclic process.

- In cyclic process workdone is zero when a graph between P-V.

- In a cyclic process there will be no change in the internal energy.

$$\text{i.e. } dU=0$$

- So $dQ = dW$ for cyclic process.

Ex : Heat engine converts to heat energy.

Non cyclic process : A process which does not attain its initial stage, it is not cyclic process. Such process is called Non-cyclic process.

- Area of curves between P-V graph can be expressed as workdone.

Ex : -Diffusion of liquids (or) gases.

- Free expansion of a perfect gas.

Problems :

1. 5 moles of H_2 . When it is heated to raise the temperature 20K at constant pressure 10^5 N/m^2 then it expands $8.3 \times 10^{-3} \text{ m}^3$ so specific heat $C_V = 20 \text{ J/mole}$ find C_P ?

Ans:-

$$C_P - C_V = R$$

with $\mu \Delta T$

$$\mu C_p \Delta T - \mu C_v \Delta T = \mu R \Delta T$$

$$\mu \Delta T (C_p - C_v) = P \Delta T \quad (\because \mu R \Delta T = P \Delta V)$$

$$5 \times 20 (C_p - C_v) = 105 \times 8.3 \times (10 - 3)$$

$$\left[\begin{array}{l} \therefore \mu = 5, \Delta T = 20\text{K}, P = 1 \times 10^5 \text{ N/m}^2 \\ C_v = 20 \text{ J/mol K and } \Delta V = 8.3 \times 10^3 \text{ m}^3 \end{array} \right]$$

$$C_p - 20 = 8.3$$

$$\therefore C_p = 28.3 \text{ J/mol.K}$$

2. How much heat is required to raise the temp 45°C of $2.0 \times 10^{-2} \text{ Kg}$ Nitrogen at room temperature, at constant pressure?

(N_2 w = 28, $R = 8.3 \text{ J/mol.K}$)

Ans:- Mass of the gas $m = 2 \times 10^{-2} \text{ Kg} = 20 \text{ g}$

Increasing temp $\Delta T = 45^\circ\text{C}$

required heat $\Delta Q = ?$

at mass of $\text{N}_2 = 28$

$$\text{at number } n = \frac{m}{M} = \frac{20}{28} = 0.714$$

Nitrogen is diatomic molar specific heat of gas at constant pressure

$$C_p = \frac{7}{2}R = \frac{7}{2} \times 8.3 \text{ J/mol K}$$

$$\Delta Q = n C_p \Delta T$$

$$= 0.714 \times \frac{7}{2} \times 8.3 \times 45 \text{ J} = 933.45 \text{ J}$$

3. One electric heater giving heat at the rate 100 W to one system. That system is working at the 75 J/sec . Then find the increasing rate of internal energy?

Ans:- Supplied heat $\Delta Q = 100 \text{ W} = 100 \text{ J/s}$

used for work $\Delta W = 75 \text{ J/s}$

$$\Delta u = ?$$

$$\therefore \Delta Q = \Delta U + \Delta W$$

$$\Delta U = \Delta Q - \Delta W$$

$$= 100 - 75$$

$$= 25 \text{ J/s}$$

4. Eating foods are kept in refrigerator at 9°C if room temp is 36°C then calculate the coefficient of performance?

Ans:- Given $T_1 = 36^{\circ}\text{C} = 36 + 273 = 309\text{K}$

$$T_2 = 10^{\circ}\text{C} = 10 + 273 = 283\text{K}$$

$$\text{Co. of performance } (\alpha) = \frac{T_2}{T_1 - T_2} = \frac{283}{309 - 283}$$

$$= \frac{283}{26} = 10.9$$



UNIT XIV

KINETIC THEORY

VERY SHORT QUESTION & ANSWERS (2 MARKS)

1. Define mean free path?

Ans:- The average distance covered by a molecule between two successive collisions is called the mean free path.

2. How does kinetic theory justify Avagadro's hypothesis and show the avaradro number in different gases is same?

Ans:- For two different gases, we have $\frac{P_1 V_1}{N_1 T_1} = \frac{P_2 V_2}{N_2 T_2} = K_B$

If P,V,T are same, then N is also same for two gases 'N' is called Avagadro's numbers. According to Avogadro's hypothesis, that the number of molecules per unit volume is same for all gases at a fixed temperature and pressure. In this way kinetic theory justify avogadro's hypothesis.

3. When does a real gas behave like an ideal gas?

Ans:- At low pressures and high temperatures real gases behave like an ideal gas.

4. The absolute temperature of a gas is increased '3' times. What will be the increase in r.m.s velocity of the gas molecule?

Ans:- case (i) : The r.m.s velocity of gas molecule $V_1 = \sqrt{\frac{3RT_1}{M}}$

case (ii) : The rms velocity of gas molecules $V_2 = \sqrt{\frac{3RT_2}{M}}$

Increase in r.m.s velocity of gas molecules

$$= V_2 - V_1$$

$$= 1.732V_1 - V_1 = 0.732V_1$$

5. What is the expression between pressure and kinetic energy of a gas molecules?

Ans:- By kinetic theory pressure $P = \frac{1}{3}mv^2$ and

Kinetic energy $= \frac{1}{2}mv^2$, Where 'm' is the mass of the molecules, n is the no. of moles per unit volume ρ - is the mean-square - speed.

$$\therefore P = \frac{2}{3} \left(\frac{1}{2}mv^2 \right)$$

$$P = \frac{2}{3} \times K.E$$

SHORT QUESTION & ANSWERS (4MARKS)

1. How specific heat capacity of mono atomic, diatomic and poly atomic gases can be explained on the basis of law of equipartition of energy?

Ans:- (i) Monoatomic gases : According to law of equipartition of energy a molecule of monoatomic gas has only '3' (translational) degree of freedom i.e $f = 3$.

The molecular specific heat of the gas at constant volume is given by $C_v = \frac{f}{2}R$ Where 'f' is degree of freedom.

$$\therefore C_v = \frac{3}{2}R = 3 \text{ cal / mol - K } (\because R = 2 \text{ cal / mole - K})$$

The molar specific heat at constant pressure is given by

$$C_p = \left(\frac{f}{2} + 1\right)R = \left(\frac{3}{2} + 1\right)R = \frac{5}{2}R = 5 \text{ cal / mol}$$

$$= 5 \text{ cal / mol - K}$$

(ii) Diatomic gases : A molecule of diatomic gas has '5' degree of freedom 3 translational and 2 rotational i.e $f = 5$.

$$\therefore C_v = \frac{f}{2}R = \frac{5}{2}R = 5 \text{ cal / mole - K}$$

$$C_p = \left(\frac{f}{2} + 1\right)R = \frac{7}{2}R = 7 \text{ cal / mole - K}$$

(iii) Polyatomic gases : Polyatomic molecules has '3' translational, 3-rotational degrees of freedom.

i.e $f = 6$

$$\therefore C_v = \frac{f}{2}R = 3R = 6 \text{ cal / mol - K}$$

$$C_p = \left(\frac{f}{2} + 1\right)R = 4R = 8 \text{ cal / mol - K}$$

2. Prove that the average K.E of a molecule of an ideal gas is directly proportional to the absolute temperature of the gas.

Ans:- Since the pressure of the gas is given by

$$P = \frac{1}{3}mn\bar{v}^2, \text{ where } m \rightarrow \text{mass of the gas}$$

$$n \rightarrow \frac{N}{V} \text{ no. of molecule per unit volume.}$$

$$\bar{v} \rightarrow \text{r.m.s velocity of gas}$$

$$\therefore p = \frac{1}{3} m \frac{N}{V} \vartheta^2$$

$$\Rightarrow PV = \frac{1}{3} m N \vartheta^2 \text{ -----(1)}$$

we know 1 gm molecule of the gas is $PV = RT$ -----(2)

$$\text{from eqn (1) \& (2) } RT = \frac{1}{3} m N \vartheta^2$$

$$\frac{3RT}{N} = m \vartheta^2$$

$$\Rightarrow \frac{3}{2} \frac{R}{N} T = \frac{1}{2} m \vartheta^2$$

$$\Rightarrow \frac{3}{2} K_B T = \frac{1}{2} m \vartheta^2 \quad \left(\because \frac{R}{N} = K_B \right)$$

Here K_B Boltzmann constant and 'T' - absolute temp.

$$\therefore \boxed{E = \frac{3}{2} K_B T} \quad \left(K.E = \frac{1}{2} m \vartheta^2 \right)$$

Hence K.E of a molecule an ideal gas is directly proportional to the absolute temperature of the gas.

LONG QUESTION & ANSWERS (8MARKS)

1. Derive an expression for the pressure of an ideal gas in a container from kinetic theory and hence give kinetic interpretation of temperature.

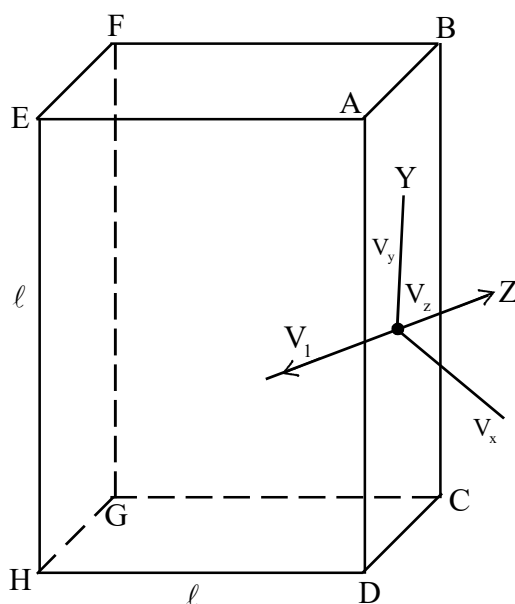
Ans:- Let us consider a cubical vessel of side ' ℓ ' with perfectly elastic wall, containing gas molecules. Let the three sides of the cube be taken as co-ordinates axis. Consider a molecule moving with velocity V_1 in any direction at any instant. The components of 'V' along the three sides are $\vartheta_x, \vartheta_y, \vartheta_z$ respectively, then

$$\vartheta_1^2 = \vartheta_x^2 + \vartheta_y^2 + \vartheta_z^2 \text{ -----(1)}$$

If 'm' is the mass of this molecule it transfers a momentum $m\vartheta_x$ when it strikes the face ABCD of the cube. Since the wall is perfectly elastic, this molecule is reflected back with a velocity - ϑ_x and momentum - $m\vartheta_x$ so the change in momentum = $m\vartheta_x - (-m\vartheta_x) = 2m\vartheta_x$.

This molecule then travels towards the opposite face. collides with it and rebounds and travels again towards the face ABCD. The distance travelled between two successive

collisions is ' 2ℓ '. Time taken between two successive collisions is $\frac{2\ell}{v}$.



$$\therefore \text{no. of collisions per second} = \frac{v_x}{2\ell}$$

$$\begin{aligned} \text{Change in momentum per one second} &= (2mv_x) \times \left(\frac{v_x}{2\ell} \right) \\ &= \frac{mv_x^2}{\ell} \end{aligned}$$

$$\text{Thes force exerted by this molecule} = \frac{mv_x^2}{\ell} \left(\because R = \frac{dp}{dt} \right)$$

hence force exerted by 'N' such molecules in the x-direction

$$f_x = N \frac{mv_x^2}{\ell} = \frac{mNv_x^2}{\ell}$$

Pressure exerted by the molecules in the x - direction is ' P_x '

$$\text{i.e. } P_x = \frac{f_x}{\ell^2} = \frac{mNv_x^2}{\ell} \times \frac{1}{\ell^2} = \frac{mNv_x^2}{\ell^3} \quad \text{-----}(2)$$

Similarly pressure exerted by the molecules in the y and z disections are

$$P_y = \frac{mNv_y^2}{\ell^3} \quad \text{-----}(3)$$

$$P_z = \frac{mNv_z^2}{\ell^3} \quad \text{-----}(4)$$

Since the pressure exerted by a gas in all the directions is same, the average pressure.

$$P = \frac{P_x + P_y + P_z}{3} = \frac{mN}{3\ell^3} [v_x^2 + v_y^2 + v_z^2]$$

$$= \frac{mN}{3V} v^2 \quad (\text{from eqn (1)})$$

$$(\because \text{cube } V = \ell^3)$$

Here ' \bar{v}^2 ' is the mean square velocity of the molecule, 'V' is the volume of the vessel.

If 'm' is the mass of the gas then $M = mN$

$$\therefore P = \frac{1}{3} \frac{m\bar{v}^2}{V} = \frac{1}{3} \frac{mN\bar{v}^2}{V} \quad \left[\because n = \frac{N}{V} \right]$$

This pressure is actually the pressure exerted by an ideal gas.

Kinetic interpretation of temperature :

Since the pressure of the gas is given by $P = \frac{1}{3} m n \bar{v}^2$

Where m = mass of the gas

$$\Rightarrow n = \frac{N}{V} \Rightarrow \text{no. of molecules per unit volume.}$$

$\Rightarrow V \rightarrow$ r.m.s velocity of gas.

$$\therefore P = \frac{1}{3} m \frac{N}{V} \bar{v}^2$$

$$\Rightarrow PV = \frac{1}{3} m N \bar{v}^2$$

We know the ideal gas for one mole $PV = RT$

$$\text{we get } RT = \frac{1}{3} m N \bar{v}^2$$

$$\frac{3RT}{N} = m \bar{v}^2 \rightarrow \text{multiply with } \frac{1}{2} \text{ on both sides}$$

$$\therefore \left[\frac{1}{2} m \bar{v}^2 = \frac{3}{2} K_B T \right] \quad \left(\because \frac{R}{N} = K_B \right)$$

Here K_B is Boltzmann constant. So mean kinetic energy of a molecule is $K_B T$. Which depends upon the temp. As temp increases mean kinetic energy of the molecules also increases.

Problems :

1. Calculate the ratio of Oxygen, Hydrogen molecules of r.m.s velocities at same temperature?

Ans:- r.m.s velocity of gas $\bar{v} = \sqrt{\frac{3RT}{M}}$

$$\Rightarrow \frac{v_O}{v_H} = \sqrt{\frac{\mu_H}{\mu_O}}$$

$$\mu_H = 2 \text{ and } \mu_O = 32$$

$$\frac{v_O}{v_H} = \sqrt{\frac{2}{32}} = \frac{1}{4}$$

$$\therefore \boxed{v_O : v_H = 1 : 4}$$

2. '4' molecules in a gas, whose velocities are 1,2,3,4 km/s respectively calculate the r.m.s velocity of gas molecule.

Ans:- $\vartheta_1 = 1 \text{ km/s}$ $\vartheta_2 = 2 \text{ km/s}$ $\vartheta_3 = 3 \text{ km/s}$ $\vartheta_4 = 4 \text{ km/s}$

$\therefore \vartheta_{\text{rms}} = ?$

$$\vartheta_{\text{rms}} = \sqrt{\frac{\vartheta_1^2 + \vartheta_2^2 + \vartheta_3^2 + \vartheta_4^2}{n}} = \sqrt{\frac{1^2 + 2^2 + 3^2 + 4^2}{4}}$$

$$= \sqrt{\frac{1+4+9+16}{4}} = \sqrt{\frac{30}{4}} = \sqrt{7.5} = 2.735 \text{ km/s}$$

3. 1 gm of Helium is at 127°C temperature then find the molecular kinetic energy? (given $R = 8.31 \text{ J/mol-K}$)

Ans:- Given data : $t = 127^\circ\text{C}$

$$T = 273 + 127 = 400, \quad R = 8.31 \text{ J/mole}$$

$$\text{K.E} = \frac{3}{2} K_B T = \frac{3}{2} \times 1.38 \times 10^{-23} \times 400 = 8.28 \times 10^{-21} \text{ J}$$

